

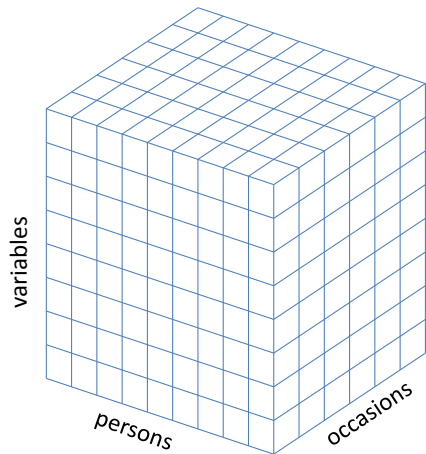
Dynamic Structural Equation Modeling of Intensive Longitudinal Data Using Mplus Version 8 (Part 1)

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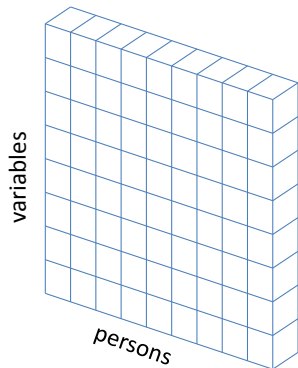
Tihomir Asparouhov & Bengt Muthén
Muthén & Muthén

PSMG, March 14, 2017

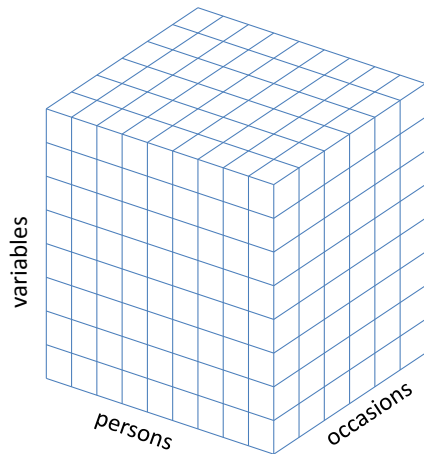
Cattell's data box



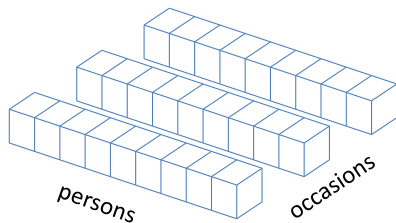
Cross-sectional research: N is large, $T=1$



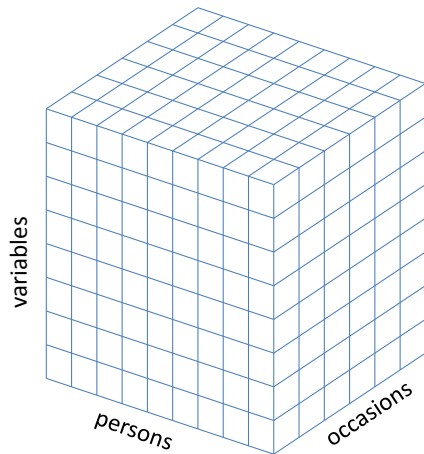
Cattell's data box



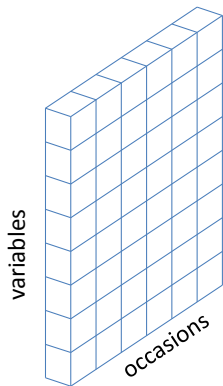
Panel research: N is large, T is small



Cattell's data box



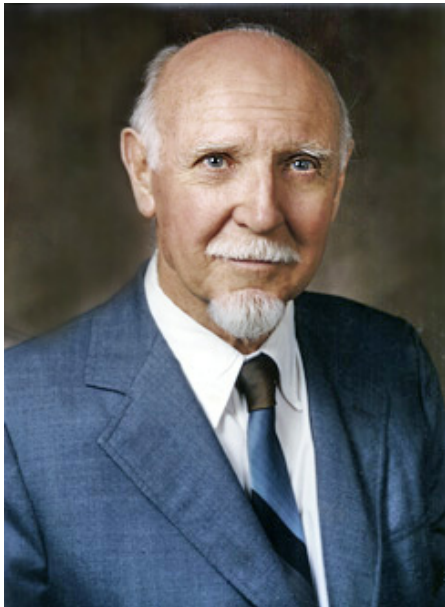
Time series data: $N=1$ and T is large



Time series analysis: Looking at the movie



Pioneers of idiographic research in psychology



Idiographic (N=1) research in psychology

N=1 research has included:

- Cattell's P-technique: factor analysis of N=1 data
- Dynamic factor analysis: considering lagged relationships
- Measurement burst design: multiple waves of intensive measurements
- Intervention research: ABAB design etc.

Critique of this kind of research:

- within-person fluctuations are just **noise**
- results are **not generalizable**
- no one has these data

New technology

Smart phones



Smart glasses



Secure continuous remote alcohol monitor (SCRAM)



Smart watches



Activity trackers



Intensive longitudinal data

Different forms of intensive longitudinal data:

- daily diary (DD); self-report end-of-day
- experience sampling method (ESM); self-report of subjective experience
- ecological momentary assessment (EMA); healthcare related self-report
- ambulatory assessment (AA); physiological measurements
- event-based measurements; self-report after a particular event
- observational measurements; expert rater

For more info on **methodology**, check out:

- Seminar of Tamlin Conner and Joshua Smyth on YouTube (<https://www.youtube.com/watch?v=nQBBVp9vBIQ>)
- Society for Ambulatory Assessment (<http://www.saa2009.org/>)
- Life Data (<https://www.lifedatacorp.com/>)
- Quantified Self (<http://quantifiedself.com/>)

Characteristics of these kind of data

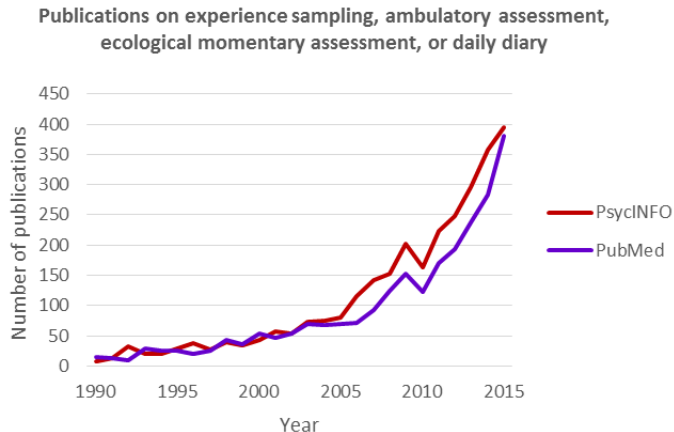
Data structure:

- one or more measurements per day
- typically for multiple days
- sometimes multiple waves (i.e., Nesselroade's measurement-burst design)

Advantages of ESM, EMA and AA

- no recall bias
- high ecological validity
- physiological measures over a large time span
- monitoring of symptoms and behavior, with new possibilities for feedback and intervention (e-Health and m-Health)
- window into the dynamics of processes

A paradigm shift



Taken from Hamaker and Wichers (2017)

Outline

- **Modeling the dynamics of ILD**
- Separating between-person and within-person variance
- Application 1: Daily negative affect and depressive symptomatology
- Application 2: Intervention study with ESM
- Conclusion

What is time series analysis?

Time series analysis is a class of techniques that is used in econometrics, seismology, meteorology, control engineering, and signal processing.

Main characteristics:

- $N=1$ technique
- T is large (say >50)
- concerned with *trends*, *cycles* and *autocorrelation structure* (i.e., serial dependency)
- goal: forecasting (\neq prediction)

Lags

| Y | Y at lag 1 | Y at lag 2 |
|-------|--------------|--------------|
| y_1 | | |
| y_2 | y_1 | |
| y_3 | y_2 | y_1 |
| y_4 | y_3 | y_2 |
| y_5 | y_4 | y_3 |
| y_6 | y_5 | y_4 |
| y_7 | y_6 | y_5 |
| y_8 | y_7 | y_6 |
| ... | ... | ... |
| y_T | y_{T-1} | y_{T-2} |
| | y_T | y_{T-1} |
| | | y_T |

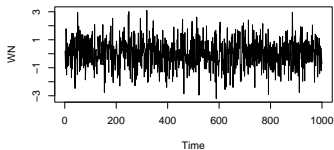
Partial autocorrelation function (PACF)

Partial autocorrelation at lag k : The correlation between y_t and y_{t-k} after **removing the effect of the intermediate observations** (i.e., y_{t-1} to y_{t-k+1}).

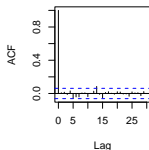
| Y | Y at lag 1 | Y at lag 2 |
|-------|------------|------------|
| y_1 | | |
| y_2 | y_1 | |
| y_3 | y_2 | y_1 |
| y_4 | y_3 | y_2 |
| y_5 | y_4 | y_3 |
| ... | ... | ... |
| y_T | y_{T-1} | y_{T-2} |
| | y_T | y_{T-1} |
| | | y_T |

Sequence, ACF and PACF

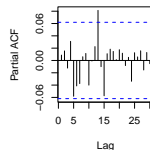
White Noise process



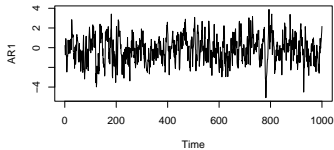
Series WN



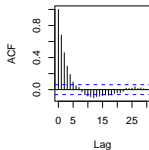
Series WN



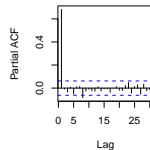
First-order AR process



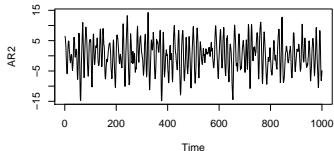
Series AR1



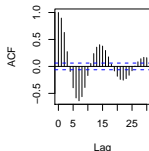
Series AR1



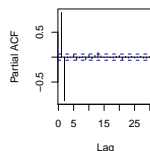
Second-order AR process



Series AR2



Series AR2

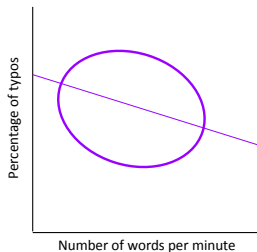


Outline

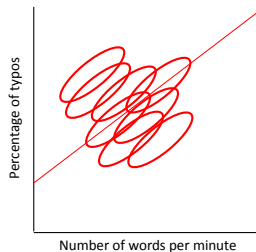
- Modeling the dynamics of ILD
- **Separating between-person and within-person variance**
- Application 1: Daily negative affect and depressive symptomatology
- Application 2: Intervention study with ESM
- Conclusion

A fundamental problem in a nutshell

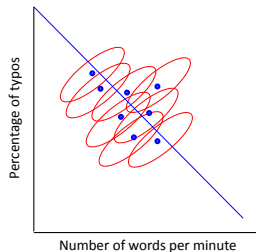
Cross-sectional relationship



Within-person relationship



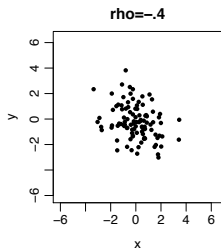
Between-person relationship



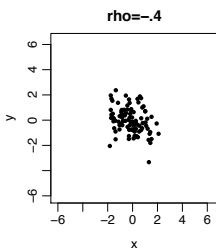
Taken from Hamaker (2012).

Three perspectives on data

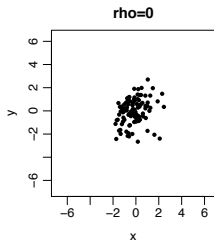
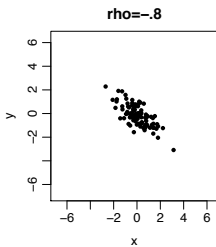
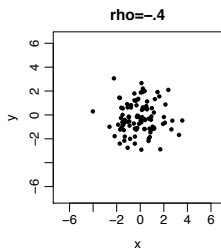
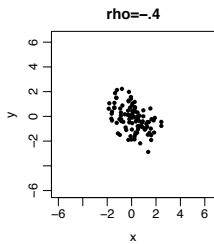
Cross-sectional



Within

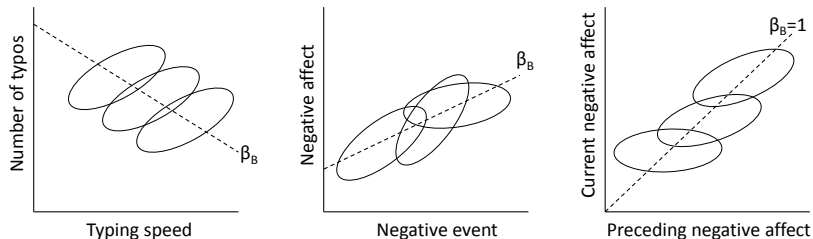


Between



Taken from Hamaker (2012).

Between-person differences in within-person slopes



Taken from Hamaker and Grasman (2014).

In conclusion: To study within-person processes we need

- (intensive) **longitudinal** data
- to **decompose** observed variance into within and between
- to consider **individual differences** in within-person dynamics

Outline

- Modeling the dynamics of ILD
- Separating between-person and within-person variance
- **Application 1: Daily negative affect and depressive symptomatology**
- Application 2: Intervention study with ESM
- Conclusion

Data: Daily measurements of negative affect (NA)

Data come from the **COGITO study** of the MPI in Berlin (based on Hamaker et al., in preparation).

Here we consider the **younger sample**:

- aged 20-31
- 101 individuals
- 100 daily measurements of negative affect (NA)

Decomposition into a between part and a within part

$$NA_{it} = \mu_i + NA_{it}^*$$

where

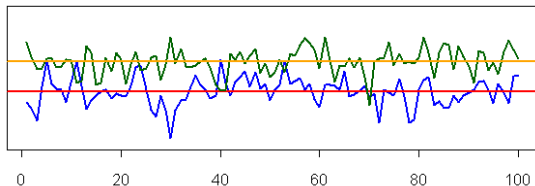
- Between part: μ_i is the individual's **mean** (i.e., baseline, trait, equilibrium)
- Within-part: NA_{it}^* is the **within-person centered** (cluster-mean centered) score

Between versus within

Here, the **intraclass correlation** is:

$$\frac{\sigma_{between}^2}{\sigma_{between}^2 + \sigma_{within}^2} = .64$$

meaning there is about twice as much variability between people as there is within people in these data.



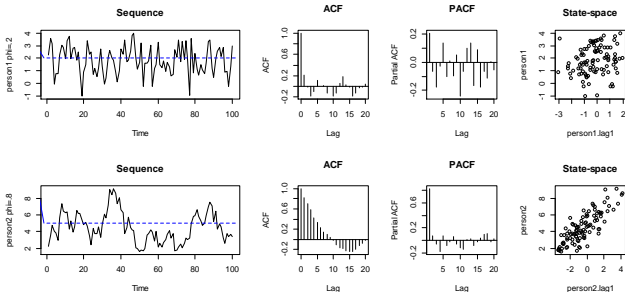
Univariate multilevel AR(1) model

Autoregressive part:

$$NA_{it}^* = \phi_i NA_{i,t-1}^* + \zeta_{it}$$

where

- ϕ_i is the **autoregressive parameter** (i.e., inertia, carry-over)
- ζ_{it} is the **innovation** (residual, disturbance, dynamic error) (with $\zeta_{it} \sim N(0, \sigma_\zeta^2)$)



Univariate multilevel AR(1) model

Within level: AR(1) with random ϕ_i

$$NA_{it}^* = \phi_i NA_{i,t-1}^* + \zeta_{it} \quad \zeta_{it} \sim N(0, \sigma^2)$$

Parameters estimated at this level: residual variance σ^2

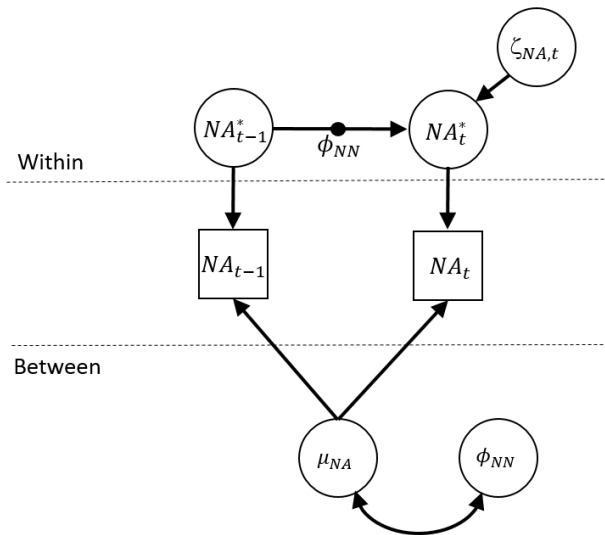
Between level: fixed and random effects

$$\begin{aligned} \mu_i &= \gamma_\mu + u_{0i} \\ \phi_i &= \gamma_\phi + u_{1i} \end{aligned} \quad \begin{bmatrix} u_{0i} \\ u_{1i} \end{bmatrix} \sim MN \left[\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \psi_{11} & \\ \psi_{21} & \psi_{22} \end{bmatrix} \right]$$

Parameters estimated at this level:

- fixed effects (means): γ_μ and γ_ϕ
- random effects (variances): ψ_{11} and ψ_{22}
- relation between random effects (covariance): ψ_{21}

Univariate multilevel AR(1) model



Mplus input

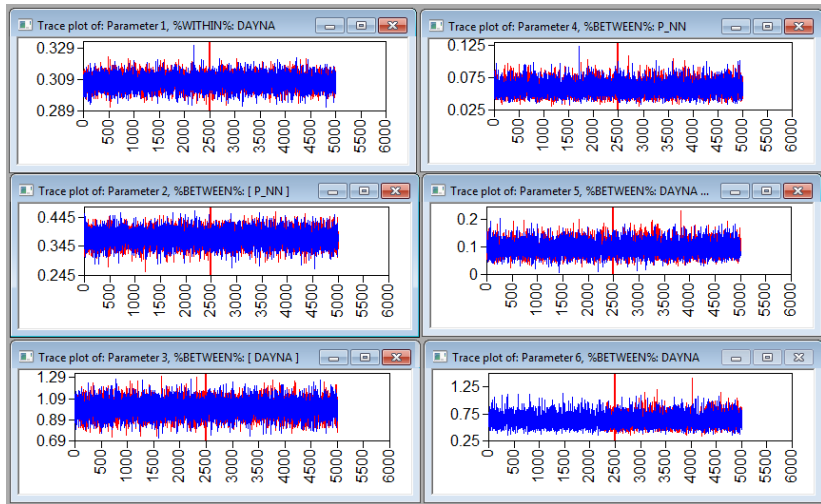
```
VARIABLE:
names          = ID sessdate na1 na2 na3 na4 na5 na6 na7 na8 na9 na10
                pa1 pa2 pa3 pa4 pa5 pa6 pa7 pa8 pa9 pa10 sessionNr
                age_pre sex CESDpre CESDpost dayNA dayPA older;
cluster        = ID;
usevar         = dayNA;
lagged         = dayNA(1);
tinterval      = sessdate(1);
missing        = all(-999);

ANALYSIS:      TYPE = twolevel random;
                estimator = bayes;
                proc = 2;
                biter= (5000);
                bseed = 526;
                thin = 10;

MODEL:
  %WITHIN%
  p_nn | dayNA ON dayNA&1;

  %BETWEEN%
  p_nn WITH dayNA;
```

Mplus results: Trace plots



Mplus results: Parameter estimates

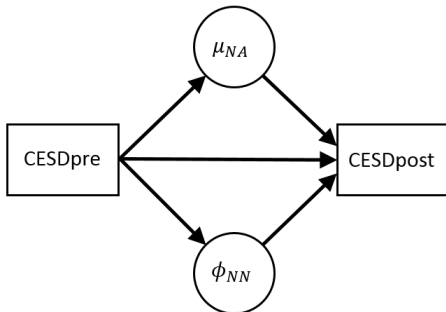
MODEL RESULTS

| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|--------------------|----------|-------------------|-----------------------|------------|------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| Within Level | | | | | | |
| Residual Variances | | | | | | |
| DAYNA | 0.307 | 0.004 | 0.000 | 0.299 | 0.316 | * |
| Between Level | | | | | | |
| P_NN WITH | | | | | | |
| DAYNA | 0.093 | 0.025 | 0.000 | 0.051 | 0.146 | * |
| Means | | | | | | |
| DAYNA | 0.998 | 0.082 | 0.000 | 0.844 | 1.163 | * |
| P_NN | 0.377 | 0.027 | 0.000 | 0.323 | 0.426 | * |
| Variances | | | | | | |
| DAYNA | 0.617 | 0.118 | 0.000 | 0.434 | 0.887 | * |
| P_NN | 0.057 | 0.010 | 0.000 | 0.041 | 0.082 | * |

Dynamic multilevel mediation model

Within level: AR(1) with random ϕ_i

$$NA_{it}^* = \phi_i NA_{i,t-1}^* + \zeta_{it} \quad \zeta_{it} \sim N(0, \sigma^2)$$



Between level: Mediation model

$$\mu_i = \gamma_\mu + \gamma_{01} CESDpre_i + u_{0i}$$

$$\phi_i = \gamma_\phi + \gamma_{11} CESDpre_i + u_{1i}$$

$$CESDpost_i = \gamma_{20} + \gamma_{21} CESDpre_i + \gamma_{22} \mu_i + \gamma_{23} \phi_i + u_{2i}$$

Mplus input mediation model

```
VARIABLE:
names      = ID sessdate na1 na2 na3 na4 na5 na6 na7 na8 na9 na10
            pa1 pa2 pa3 pa4 pa5 pa6 pa7 pa8 pa9 pa10 sessionNr
            age_pre sex CESDpre CESDpost dayNA dayPA older;
cluster    = ID;
usevar     = dayNA CESDpre CESDpost;
between    = CESDpre CESDpost;
lagged     = dayNA(1);
tinterval  = sessdate(1);
missing    = all(-999);

DEFINE: CENTER CESDpre CESDpost (GRANDMEAN);

ANALYSIS:  TYPE IS TWOLEVEL random;
           estimator=bayes; proc=2;
           fbiter=5000; bseed=1956; thin=10;

MODEL:
  %WITHIN%
  p_nn | dayNA ON dayNA&1;

  %BETWEEN%
  p_nn dayNA ON CESDpre (a1-a2);
  CESDpost ON p_nn dayNA CESDpre (b1-b3);

model constraint:
  new (ab_p_nn); ab_p_nn=a1*b1; ! MEDIATED PATH THROUGH AR PARAMETER
  new (ab_dayNA); ab_dayNA=a2*b2; ! MEDIATED PATH THROUGH WITHIN-PERSON MEAN
```

Mplus output mediation model

MODEL RESULTS

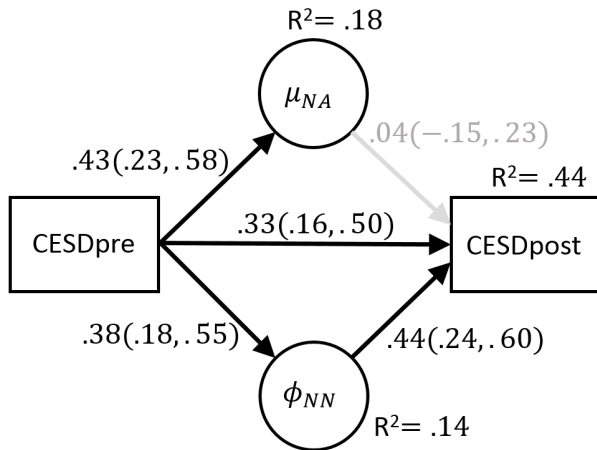
| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|---------------------------------|----------------|-------------------|-----------------------|-----------------|----------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| Within Level | | | | | | |
| Residual Variances | | | | | | |
| DAYNA | 0.307 | 0.004 | 0.000 | 0.299 | 0.316 | * |
| Between Level | | | | | | |
| P_NN ON CESDPRE | 0.254 | 0.071 | 0.000 | 0.118 | 0.397 | * |
| CESDPOST ON P_NN | 0.698 | 0.164 | 0.000 | 0.385 | 1.020 | * |
| DAYNA ON CESDPRE | 1.018 | 0.257 | 0.000 | 0.509 | 1.505 | * |
| CESDPOST ON DAYNA CESDPRE | 0.017 0.364 | 0.044 0.100 | 0.351 0.000 | -0.071 0.170 | 0.103 0.560 | * |

Mplus output mediation model

(continued)

| | | | | | | |
|---------------------------|--------|-------|-------|--------|--------|---|
| Means | | | | | | |
| CESDPRE | 0.000 | 0.035 | 0.499 | -0.067 | 0.068 | |
| Intercepts | | | | | | |
| CESDPOST | -0.281 | 0.069 | 0.000 | -0.416 | -0.144 | * |
| DAYNA | 1.002 | 0.076 | 0.000 | 0.854 | 1.157 | * |
| P_NN | 0.378 | 0.025 | 0.000 | 0.327 | 0.426 | * |
| Variances | | | | | | |
| CESDPRE | 0.119 | 0.017 | 0.000 | 0.091 | 0.159 | * |
| Residual Variances | | | | | | |
| CESDPOST | 0.081 | 0.013 | 0.000 | 0.060 | 0.111 | * |
| DAYNA | 0.552 | 0.094 | 0.000 | 0.400 | 0.768 | * |
| P_NN | 0.047 | 0.009 | 0.000 | 0.033 | 0.067 | * |
| New/Additional Parameters | | | | | | |
| AB_P_NN | 0.174 | 0.066 | 0.000 | 0.067 | 0.321 | * |
| AB_DAYNA | 0.016 | 0.046 | 0.351 | -0.069 | 0.115 | |

Mediation model: Standardized results



Random variance (cf. Jongerling et al., 2015)

Within level: AR(1) with random ϕ_i

$$NA_{it}^* = \phi_i NA_{i,t-1}^* + \zeta_{it} \quad \zeta_{it} \sim N(0, \sigma^2)$$

Where ζ is the **innovation**, consisting of:

- external influences
- reactivity to external influences

Reasons to assume **individual differences** for σ^2 :

- individuals may differ with respect to the **variability in exposure** to external factors
- individuals may differ with respect to their **reactivity** to external influences (see reward experience and stress sensitivity research)

Hence, we allow for a **random innovation variance** using a log normal distribution.

Random innovation variance

Within level: AR(1) with random ϕ_i

$$NA_{it}^* = \phi_i NA_{i,t-1}^* + \zeta_{it} \quad \zeta_{it} \sim N(0, \sigma_i^2)$$

Between level: fixed and random effects

$$\begin{aligned} \mu_i &= \gamma_\mu + u_{0i} \\ \phi_i &= \gamma_\phi + u_{1i} \\ \log(\sigma_i^2) &= \gamma_{\log(\sigma^2)} + u_{2i} \end{aligned} \quad \begin{bmatrix} u_{0i} \\ u_{1i} \\ u_{2i} \end{bmatrix} \sim MN \left[\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \psi_{11} & & \\ \psi_{21} & \psi_{22} & \\ \psi_{31} & \psi_{32} & \psi_{33} \end{bmatrix} \right]$$

MODEL :

```
%WITHIN%  
p_nn | dayNA ON dayNA&1;  
logRVNA | dayNA;  
  
%BETWEEN%  
p_nn WITH logRVNA dayNA;  
logRVNA WITH dayNA;
```

Mplus results

| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|---------------|----------|-------------------|-----------------------|------------|------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| Within Level | | | | | | |
| Between Level | | | | | | |
| P_NN WITH | | | | | | |
| LOGRVNA | 0.082 | 0.035 | 0.004 | 0.021 | 0.160 | * |
| DAYNA | 0.065 | 0.022 | 0.001 | 0.027 | 0.114 | * |
| LOGRVNA WITH | | | | | | |
| DAYNA | 0.563 | 0.113 | 0.000 | 0.379 | 0.819 | * |
| Means | | | | | | |
| DAYNA | 0.977 | 0.075 | 0.000 | 0.829 | 1.123 | * |
| P_NN | 0.406 | 0.026 | 0.000 | 0.355 | 0.456 | * |
| LOGRVNA | -1.663 | 0.118 | 0.000 | -1.905 | -1.433 | * |
| Variances | | | | | | |
| DAYNA | 0.543 | 0.086 | 0.000 | 0.408 | 0.737 | * |
| P_NN | 0.058 | 0.010 | 0.000 | 0.042 | 0.081 | * |
| LOGRVNA | 1.382 | 0.216 | 0.000 | 1.046 | 1.892 | * |

Mplus results (cf. Schuurman et al., 2016)

STDYX Standardization

| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|--|----------|-------------------|-----------------------|------------|------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |

Within-Level Standardized Estimates Averaged Over Clusters

| | | | | | | |
|----------------------------|-------|-------|-------|-------|-------|---|
| P_NN DAYNA ON DAYNA&1 | 0.405 | 0.010 | 0.000 | 0.385 | 0.425 | * |
| LOGRVNA DAYNA | 0.783 | 0.008 | 0.000 | 0.767 | 0.797 | * |

Between Level

| | | | | | | |
|-----------------------|-------|-------|-------|-------|-------|---|
| P_NN WITH LOGRVNA | 0.294 | 0.105 | 0.004 | 0.079 | 0.488 | * |
| DAYNA | 0.370 | 0.101 | 0.001 | 0.156 | 0.553 | * |
| LOGRVNA WITH DAYNA | 0.654 | 0.061 | 0.000 | 0.516 | 0.756 | * |

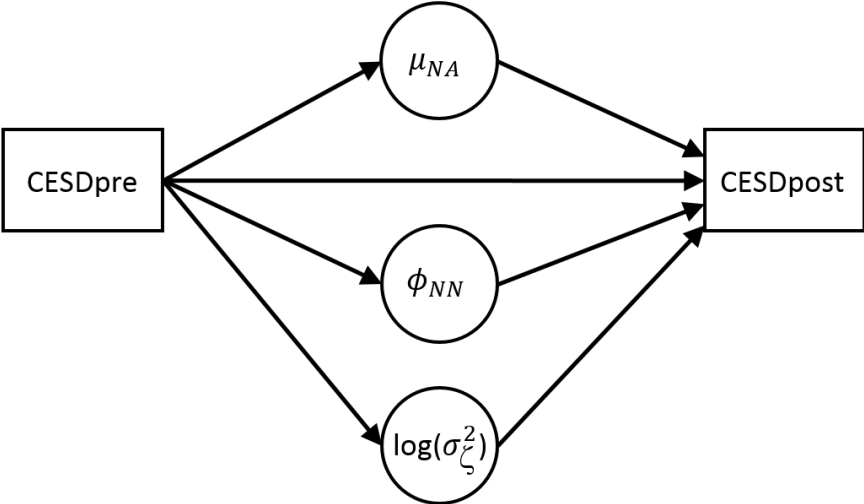
(...)

R-SQUARE

Within-Level R-Square Averaged Across Clusters

| Variable | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | |
|----------|----------|-------------------|-----------------------|------------|------------|
| | | | | Lower 2.5% | Upper 2.5% |
| DAYNA | 0.217 | 0.008 | 0.000 | 0.203 | 0.233 |

Mediation model with random innovation variance



Mediation model with random innovation variance

MODEL RESULTS

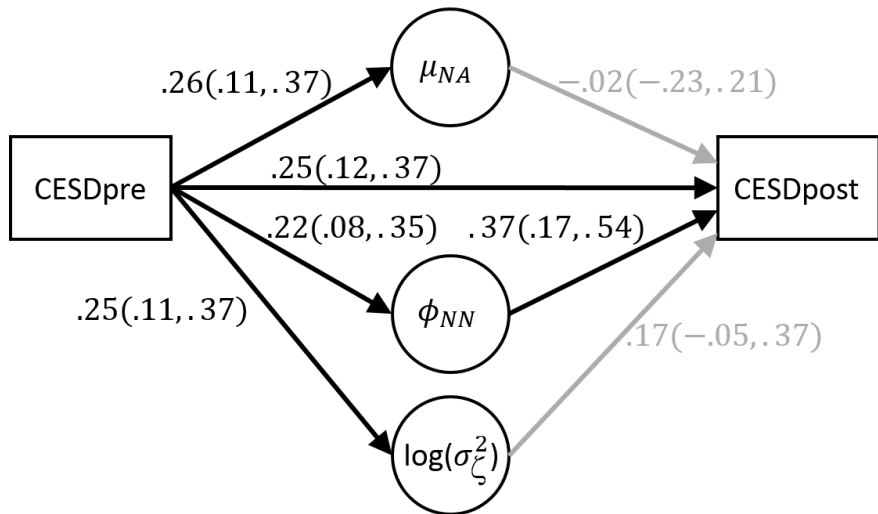
| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|-----------------------|----------|-------------------|-----------------------|------------|------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| Within Level | | | | | | |
| Between Level | | | | | | |
| P_NN ON CESDPRE | 0.213 | 0.070 | 0.002 | 0.074 | 0.350 | * |
| LOGRVNA ON CESDPRE | 1.193 | 0.326 | 0.000 | 0.556 | 1.837 | * |
| CESDPOST ON P_NN | 0.569 | 0.158 | 0.000 | 0.258 | 0.876 | * |
| LOGRVNA | 0.053 | 0.035 | 0.062 | -0.016 | 0.124 | |
| DAYNA ON CESDPRE | 0.780 | 0.231 | 0.000 | 0.332 | 1.252 | * |
| CESDPOST ON DAYNA | -0.010 | 0.058 | 0.438 | -0.126 | 0.104 | |
| CESDPRE | 0.378 | 0.099 | 0.000 | 0.181 | 0.570 | * |

Mediation model with random innovation variance

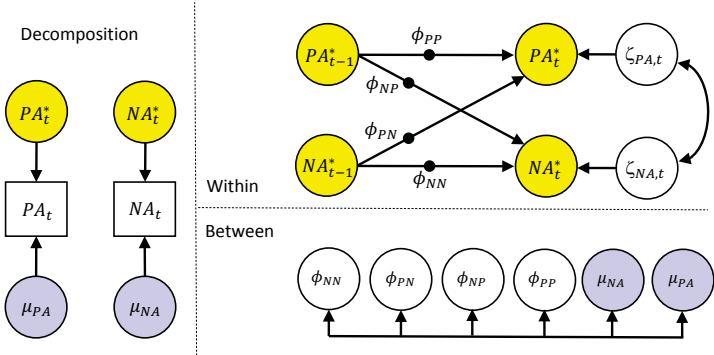
MODEL RESULTS

| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|---------------------------|----------|-------------------|-----------------------|------------|------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| (...) | | | | | | |
| Intercepts | | | | | | |
| CESDPOST | -0.134 | 0.119 | 0.133 | -0.362 | 0.103 | |
| DAYNA | 0.972 | 0.069 | 0.000 | 0.833 | 1.107 | * |
| P_NN | 0.406 | 0.025 | 0.000 | 0.358 | 0.456 | * |
| LOGRVNA | -1.664 | 0.109 | 0.000 | -1.874 | -1.446 | * |
| Residual Variances | | | | | | |
| CESDPOST | 0.086 | 0.014 | 0.000 | 0.064 | 0.117 | * |
| DAYNA | 0.459 | 0.075 | 0.000 | 0.345 | 0.633 | * |
| P_NN | 0.049 | 0.009 | 0.000 | 0.035 | 0.069 | * |
| LOGRVNA | 1.165 | 0.176 | 0.000 | 0.891 | 1.579 | * |
| New/Additional Parameters | | | | | | |
| AB_P_NN | 0.116 | 0.053 | 0.002 | 0.033 | 0.238 | * |
| AB_DAYNA | -0.007 | 0.047 | 0.438 | -0.103 | 0.088 | |
| AB_LOGRV | 0.060 | 0.047 | 0.062 | -0.017 | 0.168 | |

Mediation model with random innovation variance



Bivariate model: Multilevel vector AR(1) model



Bivariate model: Mplus code

VARIABLE:

```
names      =  ID sessdate na1 na2 na3 na4 na5 na6 na7 na8 na9 na10
              pa1 pa2 pa3 pa4 pa5 pa6 pa7 pa8 pa9 pa10 sessionNr
              age_pre sex CESDpre CESDpost dayNA dayPA older;
cluster    =  ID;
usevar     =  dayPA dayNA;
lagged     =  dayPA(1) dayNA(1);
tinterval  =  sessdate(1);
missing    =  all(-999);
```

```
ANALYSIS:  TYPE IS TWOLEVEL random; estimator=bayes;
           proc = 2; fbiter= 5000; bseed = 2359; thin = 10;
```

MODEL:

```
%WITHIN%
p_pp | dayPA ON dayPA&1;
p_pn | dayPA ON dayNA&1;
p_np | dayNA ON dayPA&1;
p_nn | dayNA ON dayNA&1;

%BETWEEN%
dayPA WITH dayNA;

p_pp WITH p_pn-p_nn dayPA dayNA;
p_pn WITH p_np-p_nn dayPA dayNA;
p_np WITH p_nn dayPA dayNA;
p_nn WITH dayPA dayNA;
dayPA WITH dayNA;
```

Mplus results: Fixed, random, and standardized

Means

| | | | | | | |
|-------|-------|-------|-------|-------|-------|---|
| DAYPA | 3.090 | 0.110 | 0.000 | 2.875 | 3.308 | * |
| DAYNA | 0.977 | 0.077 | 0.000 | 0.826 | 1.128 | * |
| P_PP | 0.334 | 0.026 | 0.000 | 0.283 | 0.387 | * |
| P_PN | 0.050 | 0.022 | 0.016 | 0.006 | 0.093 | * |
| P_NP | 0.038 | 0.015 | 0.006 | 0.008 | 0.068 | * |
| P_NN | 0.370 | 0.027 | 0.000 | 0.315 | 0.423 | * |

Variances

| | | | | | | |
|-------|-------|-------|-------|-------|-------|---|
| DAYPA | 1.178 | 0.189 | 0.000 | 0.886 | 1.618 | * |
| DAYNA | 0.595 | 0.101 | 0.000 | 0.443 | 0.832 | * |
| P_PP | 0.055 | 0.010 | 0.000 | 0.039 | 0.079 | * |
| P_PN | 0.024 | 0.006 | 0.000 | 0.014 | 0.039 | * |
| P_NP | 0.013 | 0.003 | 0.000 | 0.008 | 0.021 | * |
| P_NN | 0.062 | 0.012 | 0.000 | 0.044 | 0.089 | * |

[...]

STDYX Standardization

| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|--|----------|-------------------|-----------------------|------------|------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| Within-Level Standardized Estimates Averaged Over Clusters | | | | | | |
| P_PP DAYPA ON DAYPA&1 | 0.335 | 0.011 | 0.000 | 0.312 | 0.358 | * |
| P_PN DAYPA ON DAYNA&1 | 0.034 | 0.013 | 0.006 | 0.008 | 0.059 | * |
| P_NP DAYNA ON DAYPA&1 | 0.038 | 0.011 | 0.000 | 0.017 | 0.059 | * |
| P_NN DAYNA ON DAYNA&1 | 0.370 | 0.012 | 0.000 | 0.347 | 0.394 | * |

Outline

- Modeling the dynamics of ILD
- Separating between-person and within-person variance
- Application 1: Daily negative affect and depressive symptomatology
- **Application 2: Intervention study**
- Conclusion

Intervention study with ESM

When **ESM** is used in a **randomized controlled trial**, we can investigate whether treatment affects:

- means
- dynamics (e.g., autoregression)
- variability

Here we use data from individuals with a **history of depression** and current residual depressive symptoms (Geschwind et al., 2011).

Each ESM period consisted of 6 days, 10 beeps per day.

Here we analyze 117 participants, where 56 received a **mindfulness training** between the two phases, and 61 served as **controls**.

Treatment effect on the within-person mean

Decomposition into a between part and a within part

$$\text{Pre-treatment phase: } y_{1it} = \mu_{1i} + y_{1it}^*$$

$$\text{Post-treatment phase: } y_{2it} = \mu_{2i} + y_{2it}^*$$

Between level

$$\mu_{1i} = \alpha_1 + \beta_1 \text{Group}_i + u_{1i}$$

$$\mu_{2i} = \alpha_2 + \mu_{1i} + \beta_2 \text{Group}_i + u_{2i}$$

- β_1 are initial differences between the groups
- α_2 is the effect of time
- β_2 is the effect of treatment

MODEL:

```
%WITHIN%  
na_pre WITH na_post@0;  
  
%BETWEEN%  
na_pre ON Group;  
na_post ON na_pre@1 Group;  
na_pre WITH na_post;
```

Mplus results

| | Estimate | Posterior S.D. | One-Tailed P-Value | 95% C.I. | | Significance |
|-------------------------------|-----------------|-------------------|-----------------------|-----------------|-----------------|--------------|
| | | | | Lower 2.5% | Upper 2.5% | |
| Within Level | | | | | | |
| NA_PRE WITH NA_POST | 0.000 | 0.000 | 1.000 | 0.000 | 0.000 | |
| Variances | | | | | | |
| NA_PRE | 0.639 | 0.012 | 0.000 | 0.616 | 0.662 | * |
| NA_POST | 0.483 | 0.009 | 0.000 | 0.466 | 0.501 | * |
| Between Level | | | | | | |
| NA_PRE ON GROUP | -0.005 | 0.136 | 0.484 | -0.292 | 0.249 | |
| NA_POST ON NA_PRE GROUP | 1.000 -0.320 | 0.000 0.108 | 0.000 0.002 | 1.000 -0.539 | 1.000 -0.112 | * |
| NA_PRE WITH NA_POST | -0.157 | 0.046 | 0.000 | -0.262 | -0.082 | * |
| Intercepts | | | | | | |
| NA_PRE | 2.019 | 0.095 | 0.000 | 1.837 | 2.210 | * |
| NA_POST | 0.006 | 0.077 | 0.472 | -0.148 | 0.155 | |
| Residual Variances | | | | | | |
| NA_PRE | 0.524 | 0.078 | 0.000 | 0.402 | 0.706 | * |
| NA_POST | 0.324 | 0.050 | 0.000 | 0.247 | 0.439 | * |

Treatment effect on autoregression

Within level

$$\text{Pre-treatment phase: } y_{1it}^* = \phi_{1i} y_{1it}^* + \zeta_{it}$$

$$\text{Post-treatment phase: } y_{2it}^* = \phi_{2i} y_{2it}^* + \zeta_{it}$$

Between level: Pre-treatment phase

$$\mu_{1i} = \alpha_1 + \beta_1 \text{Group}_i + u_{1i}$$

$$\phi_{1i} = \gamma_1 + \delta_1 \text{Group}_i + v_{1i}$$

We expect β_1 and δ_1 to be zero.

Between level: Post-treatment phase

$$\mu_{2i} = \alpha_2 + \mu_{1i} + \beta_2 \text{Group}_i + u_{2i}$$

$$\phi_{2i} = \gamma_2 + \phi_{1i} + \delta_2 \text{Group}_i + v_{2i}$$

- α_2 and γ_2 represent the effects of time
- β_2 and δ_2 represent the effects of treatment

Mplus results

Between Level

| | | | | | | | |
|--------------------|----|--------|-------|-------|--------|-------|---|
| PHI2 | ON | | | | | | |
| PHI1 | | 1.000 | 0.000 | 0.000 | 1.000 | 1.000 | |
| PHI2 | ON | | | | | | |
| GROUP | | -0.056 | 0.042 | 0.095 | -0.141 | 0.025 | |
| PA_PRE | ON | | | | | | |
| GROUP | | -0.199 | 0.150 | 0.090 | -0.497 | 0.094 | |
| PA_POST | ON | | | | | | |
| PA_PRE | | 1.000 | 0.000 | 0.000 | 1.000 | 1.000 | |
| GROUP | | 0.481 | 0.122 | 0.000 | 0.246 | 0.736 | * |
| Means | | | | | | | |
| PHI1 | | 0.465 | 0.019 | 0.000 | 0.427 | 0.504 | * |
| Intercepts | | | | | | | |
| PA_PRE | | 3.824 | 0.102 | 0.000 | 3.628 | 4.031 | * |
| PA_POST | | -0.067 | 0.085 | 0.208 | -0.239 | 0.104 | |
| PHI2 | | 0.002 | 0.032 | 0.481 | -0.062 | 0.060 | |
| Variances | | | | | | | |
| PHI1 | | 0.019 | 0.004 | 0.000 | 0.013 | 0.030 | * |
| Residual Variances | | | | | | | |
| PA_PRE | | 0.632 | 0.093 | 0.000 | 0.472 | 0.846 | * |
| PA_POST | | 0.356 | 0.059 | 0.000 | 0.264 | 0.493 | * |
| PHI2 | | 0.017 | 0.007 | 0.000 | 0.006 | 0.033 | * |

Mplus results (with fixed change in ϕ)

Between Level

| | | | | | | | |
|--------------------|----|--------|-------|-------|--------|--------|---|
| PHI2 | ON | | | | | | |
| PHI1 | | 1.000 | 0.000 | 0.000 | 1.000 | 1.000 | |
| PHI1 | ON | | | | | | |
| GROUP | | 0.049 | 0.045 | 0.140 | -0.041 | 0.139 | |
| PHI2 | ON | | | | | | |
| GROUP | | -0.067 | 0.032 | 0.023 | -0.132 | -0.001 | * |
| NA_PRE | ON | | | | | | |
| GROUP | | -0.046 | 0.126 | 0.361 | -0.308 | 0.189 | |
| NA_POST | ON | | | | | | |
| NA_PRE | | 1.000 | 0.000 | 0.000 | 1.000 | 1.000 | |
| GROUP | | -0.280 | 0.104 | 0.002 | -0.477 | -0.070 | * |
| Intercepts | | | | | | | |
| NA_PRE | | 2.007 | 0.088 | 0.000 | 1.839 | 2.180 | * |
| NA_POST | | 0.014 | 0.072 | 0.421 | -0.125 | 0.152 | |
| PHI1 | | 0.445 | 0.032 | 0.000 | 0.381 | 0.506 | * |
| PHI2 | | -0.013 | 0.022 | 0.280 | -0.055 | 0.032 | |
| Residual Variances | | | | | | | |
| NA_PRE | | 0.449 | 0.068 | 0.000 | 0.339 | 0.603 | * |
| NA_POST | | 0.257 | 0.043 | 0.000 | 0.189 | 0.356 | * |
| PHI1 | | 0.042 | 0.007 | 0.000 | 0.031 | 0.059 | * |
| PHI2 | | 0.001 | 0.000 | 0.000 | 0.001 | 0.001 | |

Outline

- Modeling the dynamics of ILD
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Conclusion

- DSEM in Mplus version 8 offers many new modeling opportunities for analyzing ILD
- There are many additional options not covered here
- We are working on regime-switching extensions
- We (the research community) need to gain new knowledge about these models

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