Growth Modeling With Nonignorable Dropout:
Alternative Analyses of the STAR*D Antidepressant Trial

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This article uses a general latent variable framework to study a series of models for nonignorable missingness due to dropout. Nonignorable missing data modeling acknowledges that missingness may depend not only on covariates and observed outcomes at previous time points as with the standard missing at random assumption, but also on latent variables such as values that would have been observed (missing outcomes), developmental trends (growth factors), and qualitatively different types of development (latent trajectory classes). These alternative predictors of missing data can be explored in a general latent variable framework with the Mplus program. A flexible new model uses an extended pattern-mixture approach where missingness is a function of latent dropout classes in combination with growth mixture modeling. A new selection model not only allows an influence of the outcomes on missingness but allows this influence to vary across classes. Model selection is discussed. The missing data models are applied to longitudinal data from the Sequenced Treatment Alternatives to Relieve Depression (STAR*D) study, the largest antidepressant clinical trial in the United States to date. Despite the importance of this trial, STAR*D growth model analyses using nonignorable missing data techniques have not been explored until now. The STAR*D data are shown to feature distinct trajectory classes, including a low class corresponding to substantial improvement in depression, a minority class with a U-shaped curve corresponding to transient improvement, and a high class corresponding to no improvement. The analyses provide a new way to assess drug efficiency in the presence of dropout.

Keywords: latent trajectory classes, random effects, survival analysis, not missing at random

This article considers growth modeling of longitudinal data with missingness in the form of dropout that may be nonignorable. Nonignorable missing data modeling acknowledges that missingness may depend on not only covariates and observed outcomes at previous time points as with the standard missing-at-random (MAR) assumption (Little & Rubin, 2002) customarily made in multivariate analysis software. Missingness may also depend on latent variables such as values that would have been observed (missing outcomes), developmental trends (growth factors), and qualitatively different types of development (latent trajectory classes). Many different missing data models for such situations have been presented in recent years (e.g., Albert & Follmann, 2009; Beunckens, Molenberghs, Verbeke, & Mallinckrodt, 2008; Dantan, Prout-Lima, Letenneur, & Jacqmin-Gadda, 2008; Little, 2009; Roy & Daniels, 2008; Yuan & Little, 2009). The proposed models use both continuous latent variables in the form of random effects and categorical latent variables in the form of finite mixtures.

Because missing data models draw on untestable distributional assumptions about missing data, it is important to do a sensitivity analysis with several different models. To this aim, this article uses a general latent variable framework summarized in Muthe´n and Asparouhov (2009) to explore and compare a series of key models proposed in the literature as well as several new models. To illustrate the various models, analyses are performed on data from the trial Sequenced Treatment Alternatives to Relieve Depression (STAR*D). Comparisons of models on a given data set have been hampered by lack of software development for general missing data analyses, with software typically presented for only a few model variations considered in the authors’ article. The latent variable framework of Muthe´n–Asparouhov is implemented in the Mplus software (Muthe´n & Muthe´n, 2010), which was used for all analyses in the article. Estimation is carried out with maximum likelihood through the expectation–maximization algorithm as described in Muthe´n and Asparouhov. Mplus scripts for the analyses are available online (http://www.statmodel.com/examples/penn.shtml#stard).

STAR*D is the largest antidepressant clinical trial in the United States to date. Nevertheless, analyses using modern missing data techniques have not been performed until now. In the STAR*D data, latent variable mixture modeling can play a role not only in accounting for different classes of missing data but also in studying different classes of drug response. A basic hypothesis is that the population of subjects consists of a mixture of individuals who do and do not respond to a drug. The growth models discussed here shed light on the prevalence of these mixture classes. It is argued that such use of information from the full longitudinal data offers an advantage over current antidepressant trial definitions of drug response.
response. The growth model analyses show that there are well-defined responder and nonresponder classes. Additionally, a class of subjects is found to have a U-shaped trajectory showing large, but only transient, improvement. This is of clinical importance in that unsustained early improvement with a given medication may lead a subject to prematurely discontinue treatment altogether.

The next section describes the missing data features of the STAR*D data. Following this, conventional pattern-mixture and selection missing data modeling are applied to STAR*D. The next sections consider modeling with a mixture of latent subgroups of subjects. First, growth mixture modeling under MAR is applied to the STAR*D data. Second, existing mixture pattern-mixture and mixture selection models are applied. Third, new mixture pattern-mixture and mixture selection model extensions are applied. Finally, the proposed models for STAR*D are compared by introducing a new type of model that includes the ultimate outcome of the study.

The STAR*D Antidepressant Clinical Trial

STAR*D is a multisite clinical trial of 4,041 outpatients ages 18–75 diagnosed with major depressive disorder (Rush et al., 2004; Trivedi et al., 2006). Subjects were treated with citalopram, a selective serotonin reuptake inhibitor. There was no placebo group. The current analyses focus on subjects going through the 12-week Level 1 treatment step of STAR*D, with depression severity repeatedly measured by a summed score from the 16-item Quick Inventory of Depressive Symptoms–Clinician Rated (QIDS-C, or QIDS for short) with a range of 0–27. The Level 1 visit schedule included baseline and Weeks 2, 4, 6, 9, and 12. Of the 4,041 subjects, 995 had complete data for all six occasions, 420 dropped out after the baseline, 299 dropped out after Week 2, 301 dropped out after Week 4, 484 dropped out after Week 6, and 983 dropped out after Week 9. In this way, 62% of the subjects had a dropout missing data pattern, 14% had nondropout intermittent missingness, and 25% had complete data for all six occasions. The coverage at baseline and Weeks 2, 4, 6, 9, and 12 was 1.00, .79, .69, .68, .57, and .39, respectively.

In the clinical trial literature, dropout refers to a subject who leaves the trial and on whom no further data are available. In STAR*D, some subjects left Level 1 treatment because of medication intolerance and were moved to Level 2 treatment. In the context of the clinical trial, these subjects were not considered dropouts because they continued on a different treatment. For the purposes of the statistical analyses presented here, however, these subjects are considered to be dropouts because of the absence of further Level 1 data.

STAR*D distinguished between three Level 1 endpoint categories of subjects: Subjects were moved to the next level if the medication was ineffective or not tolerated (35%), subjects were moved to follow-up if showing remission (37%), and subjects exited the study for unknown reasons (28%). Here remission was defined as a Hamilton-D score of ≤7 and, if not available, a self-reported QIDS score of ≤5 (Hamilton-D was measured only at baseline and end of Level 1). The percentage of dropouts in the three Level 1 endpoint categories were 61% (next level), 35% (follow-up), and 95% (exit study). Figure 1 shows the mean curve over the six time points for the total sample and for subjects in each of the three Level 1 endpoint categories. The figure also includes the average score among those who did and did not drop out at the next time point. It is seen that for the next-level category subjects with higher depression scores tend to drop out, whereas for the follow-up category less depressed subjects tend to drop out.

The MAR (Little & Rubin, 2002) assumption of dropout as a function of the observed QIDS outcome is not necessarily fulfilled for subjects in any of the three Level 1 endpoint categories. Variables not measured or not included in the model, that is, latent variables, may affect missingness. Some subjects may leave Level 1 because of not tolerating the medication, unrelated to the level of depression. Some subjects may leave the study for unknown reasons. Also, remission (moving subjects to follow-up) was typically determined by Hamilton-D, not the clinician-rated score used as the outcome in the analysis; Hamilton-D could not be used as the analysis outcome because it was measured only at baseline and end of Level 1. Modeling that explores possibly nonignorable missing data is therefore of interest in order to draw proper inference to the population of subjects entering Level 1.

It should be emphasized that inference from the STAR*D study is limited by having no placebo group. There are no treatment groups to be compared during the Level 1 phase considered here. Muthén and Brown (2009) have shown how randomized designs with a placebo group enable causal effect estimation using growth mixture modeling, where placebo response can be taken into account. For studies with this design, the missing data modeling to be discussed here can be combined with the Muthén–Brown approach.

Pattern-Mixture and Selection Modeling

Growth modeling analyses based on maximum likelihood estimation typically use the assumption of MAR (Little & Rubin, 2002). This covers situations where dropout is predicted by previously observed outcome values. Missing data due to dropout may not, however, fulfill the MAR assumption but may call for missing data techniques that handle nonignorable missingness, sometimes referred to as not missing at random (NMAR). NMAR arises if unobserved variables that are correlated with the outcome predict missingness, such as a high or low outcome value that is not recorded because the subject drops out. NMAR situation can be handled by using a “full-data” likelihood analysis that considers data not only the outcomes but also 0 and 1 missing data indicators for each time point (see, e.g., Little, 2009). Consider the full-data likelihood in symbolic form where y refers to the outcome vector and m refers to the binary missing data indicators:

\[ [y, m] = [m] [y|m], \]  
\[ = [y] [m|y], \]  

where the first expression refers to the pattern-mixture modeling approach (see, e.g., Little, 1995) and the second expression to the selection modeling approach (see, e.g., Diggle & Kenward, 1994). Shared-parameter modeling considers the likelihood factorization

\[ [y, m] = \sum_c [c] [m|c] [y|c]. \]
where \( c \) represents latent class variables influencing both the outcomes \( y \) and the missingness indicators \( m \). Shared-parameter modeling may also use latent variables in the form of random effects, replacing the sum in Equation 3 with integrals. It should be noted that each NMAR model involves untestable assumptions due to missing data. It is therefore important to compare results from several different models to achieve a sensitivity analysis. Recent overviews of NMAR modeling are given in Albert and Follmann (2009) and Little (2009). In longitudinal studies, the nonignorability concern is typically focused on missing data in the form of dropout, not intermittent missingness. This is also the focus of this study.

**Pattern-Mixture Modeling**

Pattern-mixture modeling (see, e.g., Demirtas & Schafer, 2003; Hedeker & Gibbons, 1997; Little, 1995) considers the likelihood factorization \([y, d] = [y|d]] [d]\), where the \( d \) variables can be represented by dummy variables for dropout occasion. A simple version of the model allows the random-effect means to vary as a function of the dropout dummy variables. A quadratic growth model is used for STAR*D.

To facilitate understanding and comparisons of the alternative missing data models, the statistical description of the modeling is complemented by model diagrams. The pattern-mixture model is
shown in diagram form in Figure 2, where squares represent observed variables and circles latent variables. Here $y_0$-$y_5$ represent the depression outcomes at baseline and through Week 12, whereas $i$, $s$, and $q$ represent the random intercept, slope, and quadratic slope. Note that these model diagrams are not geared toward causal inference. Single-headed arrows simply represent regression relationships, and double-headed arrow represent correlations. The goal of the modeling is not to draw inference on causal effects but to understand important sources of variation in the depression outcomes over time.

The $y_0$-$y_5$ outcomes show a total of 34 missing data patterns in the total sample of 4,041. The dummy dropout indicators $d_t$ are defined as $d_t = 1$ for a subject who drops out after time $t - 1$ ($t = 1, 2, \ldots, 5$) for the six time points. In the STAR*D data, the frequencies of $d_1$ are 420 ($d_1$), 229 ($d_2$), 301 ($d_3$), 484 ($d_4$), and 983 ($d_5$). There are 995 subjects who have all $d$s equal to zero, that is, do not drop out. The five dummy dropout indicators thereby define six subgroups of subjects. Intermittent missingness is observed for 559 subjects. These subjects are spread among five of the six subgroups, excluding the $d_t = 1$ subgroup. Missing data are recorded for each subject and outcome variable. This implies that within each of the six subgroups, a subject with intermittent missingness is treated the same as a subject with complete data up to that point.

The pattern-mixture model typically needs restrictions on the parameters across dropout patterns. For example, with individuals dropping out after the first time point, the linear and quadratic slope means are not identified, and for individuals dropping out after the second time point, the quadratic slope mean is not identified. In the current application of pattern-mixture modeling, these means are held equal to those of the pattern corresponding to dropping out one time point later. The random-effect mean estimates are mixed over the patterns. This mixture can then be compared to the conventional single-class model estimated under MAR. The resulting estimated mean curve is shown in Figure 3. It is seen that the estimated mean QIDS depression score at Week 12 is somewhat higher with pattern-mixture modeling than with MAR, as would be expected if dropouts have higher QIDS score. The Week 12 QIDS standard deviation is 5.3, so that the difference is approximately half a standard deviation.

**Selection Modeling**

Selection modeling uses the likelihood factorization $[y, d] = [y] [dy]$, where the $d$s are survival indicators. An often cited model for selection modeling is the one proposed by Diggle and Kenward (1994). A common form of the Diggle–Kenward selection model assumes the logistic regression model for dropout:

$$
\log \left( \frac{P(d_t = 1 | y_{0i}, y_{t-1}, 0)}{P(d_t = 0 | y_{0i}, y_{t-1}, 0)} \right) = \alpha_i + \beta_1 y_{si} + \beta_2 y_{ti-1}, \quad (4)
$$

where the $d$ variables are scored as discrete-time survival indicators, obtaining the value 0 for periods before the dropout event occurs, 1 at the time the dropout occurs, and missing for the periods after the event occurs (Muthe´n & Masyn, 2005). Here $y_{si}$ is missing for an individual who has $d_{si} = 1$, that is, drops out after $t - 1$. According to this model, MAR holds if $\beta_1 = 0$, that is, if dropout is a function of the last observed $y$ value, not the current latent $y$ value.

To complete the model, a quadratic growth curve is used as before for the STAR*D data. The model is shown in diagram form in Figure 4. Circles within squares represent variables that are not observed for the subjects who drop out. Applying the Diggle–Kenward model to the STAR*D data shows a significant positive maximum likelihood estimate of $\beta_1$. The significance of $\beta_1$ suggests that NMAR modeling is of interest. The estimated mean depression curve for the Diggle–Kenward model is seen in Figure 3, showing a trajectory similar to that of the pattern-mixture model.

**Model Assumptions**

It should be noted that MAR, pattern-mixture, and Diggle–Kenward selection modeling use different assumptions. It is instructive to consider the Diggle–Kenward model. If the model is correctly specified, $\beta_1 \neq 0$ in Equation 4 may be viewed as an indication of NMAR. This, however, relies on the Diggle–Kenward model’s untestable assumptions about the selection process (Equation 4) and the normality assumptions that are made for unobserved variables. As stated by Little (1994):

Consider a single drop-out time, and let $Y_i$ denote the (fully observed) variables up to drop-out and $Y_i$ the (incompletely observed) variables after drop-out. The data clearly supply no direct information about the distribution of $Y_i$ given $Y_i$ for subjects who drop out. Differences in the distribution of $Y_i$ given $Y_i$ for those who do and do not drop out are solely determined by distributional assumptions of the model, such as the form of the model for drop-outs, normality, or constraints on the mean and covariance matrix. (p. 86)

Considering “the distribution of $Y_i$ given $Y_i$ for those who do and do not drop out” implies a conditioning on dropout, which means that the assumption of logistic regression for dropout is involved. Consequently, $\beta_1 \neq 0$ cannot be seen as a test rejecting MAR because assumptions not included in MAR are added in the Diggle–Kenward model.

MAR also makes normality assumptions for the outcomes that are untestable for the outcomes after dropout. But the MAR assumptions do not involve a logistic regression for outcomes. Pattern-mixture also makes normality assumptions for the outcomes, but the normality is conditional on dropout patterns. All in

![Figure 2. Pattern-mixture modeling (ds are dropout dummy variables).](image-url)
all, this implies that none of the models is a special case of the other. The models should all be applied and results compared.

**MAR Modeling With Latent Subgroups of Subjects**

In the context of the STAR*D depression example, the basic psychiatric hypothesis postulates a mixture of subjects who do and do not respond to the drug. In other words, there is a hypothesis of a latent class variable underlying the outcomes. This means that the conventional, single-class pattern-mixture and selection models are insufficient modeling tools for this example. Selection and shared-parameter modeling using a latent class variable has been suggested in the literature, but the emphasis has not been so much on recovering substantively motivated trajectory classes as on representing nonignorable missingness. Pattern-mixture modeling with a latent class variable has also been suggested in the literature, but merely to better summarize dropout patterns. In this section the MAR assumption is used, and a description is given of growth mixture modeling with substantively motivated trajectory classes. Later sections return to the study of growth mixtures in the context of pattern-mixture and selection modeling.

Of psychiatric concern in antidepressant trials such as STAR*D is to identify subjects who show either “remission,” that is, have reached a sufficiently low depression level by the end of the trial, or “response,” that is, have significantly dropped in depression level since baseline. The psychiatric definition of remission is in this case a Hamilton-D score of $\leq 7$ or a self-reported QIDS score of $\leq 5$. Response is defined as a drop of at least 50% in the score from baseline. Such definitions are to some degree arbitrary, and slightly different cut-points can give quite different results. The approach may also suffer from large individual variability in the outcomes over time. Muthén, Brown, Hunter, Cook, and Leuchter (2010) and Muthén and Brown (2009) used growth mixture modeling to define instead response as the percentage of subjects in a latent trajectory class with a distinctly low trajectory mean toward the end of the trial. This has the advantage of using information from all time points and focusing on trajectory shape. Growth mixture modeling combines random-effects modeling in conventional repeated measures analysis with finite mixture modeling using latent class variables to represent qualitatively different classes of trajectories (Muthén & Shedden, 1999; Muthén & Asparouhov, 2009; Muthén et al., 2002). Growth mixture modeling is currently used in a wide variety of settings (see, e.g., Lin, Turnbull, McCulloch, & Slate, 2002, for an application to the joint study of prostate-specific antigen development and prostate cancer survival; Elliott, Gallo, Ten Have, Bogner, & Katz, 2005, for an application to identifying trajectories of positive affect and negative events following myocardial infarction; Beunckens et al., 2008, for an application to nonignorable missing data modeling in a depression trial; Muthén & Brown, 2009, for an application to the estimation of drug effects in the presence of placebo response).
Mixture modeling with missing data is also used in the context of models assuming latent ignorability as applied to noncompliance in randomized trials (see, e.g., Frangakis & Rubin, 1999; Mealli, Imbens, Ferro, & Bigger, 2004; Mutheén, Jo, & Brown, 2003).

Consider a quadratic growth mixture model with a latent trajectory class variable \( c \) assuming values \( k = 1, 2, \ldots, K \),

\[
y_{i,k} = \eta_{1k} + \eta_{2k} (a_i - \bar{a}) + \eta_{3k} (a_i - \bar{a})^2 + \epsilon_{ik},
\]

where the random-effects distributions are allowed to vary as a function of the trajectory classes \( k \):

\[
\eta_{1k} \mid c_i = \alpha_{1k} + \xi_{1k},
\]

\[
\eta_{2k} \mid c_i = \alpha_{2k} + \xi_{2k},
\]

\[
\eta_{3k} \mid c_i = \alpha_{3k} + \xi_{3k}.
\]

The residuals \( \xi_i \) have zero means and a \( 3 \times 3 \) covariance matrix \( \Psi_\xi \), here taken to be constant across the latent classes. The residuals \( \epsilon_{ik} \) have zero means and a \( T \times T \) covariance matrix \( \Theta_\epsilon \), here taken to be constant across classes as well. All residuals are assumed independently and identically distributed and normally distributed. As an alternative, a two-piece growth model can be used with a first linear piece describing early drug response during the first 2 weeks as in Uher et al. (2010) and Hunter, Mutheén, Cook, and Leuchter (2009). The one-piece model is chosen here for simplicity and because the two-piece model simply gives an elaboration with an additional minor class showing early response that at Week 12 coincides with the low class of the one-piece model. There was no evidence of a need for class-varying covariance matrices. As seen in Table 1, one to six latent classes were studied. The conventional one-class model is clearly superseded by multiclass models as judged by the Bayesian information criterion (BIC). After four classes BIC decreases very little, and the five- and six-class solutions offer only variations on the trajectory shapes found with four classes. The four-class model is therefore considered here.

The four-class Gaussian mixture model solution estimated under MAR is shown in Figure 5. The classes are well separated with a within-class standard deviation at Week 12 of 2.42. From a substantive point of view, three of the four classes are of particular interest. It is seen that an estimated 55% of the subjects are in a distinct, low class (Class 2) showing drug response. An estimated 15% are in a high, nonresponder class (Class 4). A minority class of 3% (Class 1) shows rapid initial improvement through Week 6 with later worsening, a U-shaped curve that corresponds to transient improvement and possibly placebo-only response (Mutheén & Brown, 2009). Placebo responders do not benefit from the drug but may benefit from the attention of the staff. The small size of the class, however, makes interpretation of this class questionable, and it is of interest to see whether NMAR modeling alternatives find this class.

The growth mixture modeling makes it clear that the single-class analyses using pattern-mixture and selection modeling shown in Figure 3 give a representation of the course of depression that is insufficient from a substantive point of view. The growth mixture modeling presented so far, however, assumes MAR and needs to be generalized to accommodate nonignorable missingness as discussed in the sections to follow.

### Existing NMAR Models With Latent Subgroups of Subjects

This section explores the STAR*D data with key NMAR models with latent subgroups of subjects suggested in the literature. First, a latent class version of the pattern-mixture model due to Roy (2003) is presented. Second, the Beunckens et al. (2008) mixture selection model model is presented.

#### Roy Latent Dropout Pattern-Mixture Modeling

The conventional pattern-mixture approach has been criticized in Roy (2003):

One modeling approach is to assume the distribution . . . is a mixture over dropout patterns. However, this may lead to bias due to misclassification (i.e., by assuming every subject with the same dropout time has a common distribution). In addition, when there are a large number of unique patterns, this leads to sparse strata. In that case, pattern-mixture models require further restrictions on the parameters for identifiability. (p. 830)

As an alternative to the conventional pattern-mixture model, Roy (2003) proposed a latent dropout pattern-mixture model using a latent class variable that is influenced by dropout time and influences the random-effect means for the outcomes. Here dropout time is a single covariate coded with discrete values. Instead of dropout time, Dantan et al. (2008) suggested using dummy variables for dropout occasion. With this model applied to the STAR*D data, there is little difference in results between using dropout time and using dropout dummy variables. The Roy model implies a growth mixture model as in Equations 5–8. Latent class membership is specified as a multinomial logistic regression using the dropout dummy variables as covariates:

\[
P(c_j \mid d_1, \ldots, d_T) = \frac{e^{\gamma c_j} \sum_i e^{\gamma d_i} d_i}{\sum_k e^{\gamma c_k} \sum_i e^{\gamma d_i} d_i}.
\]

This shows that the Roy latent dropout model can be seen as both a pattern-mixture type model and a shared-parameter model. Figure 6 shows the model diagram. Because of Equation 9, the arrows from the dropout dummies point to the latent class variable and therefore indirectly to the outcomes.

### Table 1

**Summary of Maximum Likelihood Results for Growth Modeling, Assuming Missing at Random and Using a Conventional One-Class Model as Well as a Growth Mixture Model With Two to Six Classes**

<table>
<thead>
<tr>
<th>Number of classes</th>
<th>Log-likelihood</th>
<th>Number of parameters</th>
<th>BIC</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-45137</td>
<td>15</td>
<td>90396</td>
</tr>
<tr>
<td>2</td>
<td>-44961</td>
<td>19</td>
<td>90081</td>
</tr>
<tr>
<td>3</td>
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<td>4</td>
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<td>27</td>
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<td>90004</td>
</tr>
<tr>
<td>6</td>
<td>-44852</td>
<td>35</td>
<td>89996</td>
</tr>
</tbody>
</table>

**Note.** BIC = Bayesian information criterion.
It should be emphasized that although the Roy model uses latent subgroups of subjects, the conceptualization of these subgroups is different from that of the growth mixture model in the previous section. Roy (2003) views the formation of latent subgroups as a better dropout classification of subjects than using observed dropout time. In contrast, growth mixture modeling views the latent subgroups as representing different outcome trajectory types, which may or may not be related to dropout time. As argued below, in a section that presents a new type of Roy model, the latent subgroup formation in Roy is influenced not only by dropout time but also by trajectory type, and this makes the interpretation of results from the Roy model less clear-cut.

Table 2 shows the log-likelihood, number of parameters, and BIC values for the conventional pattern-mixture model and the Roy latent dropout model for $K = 2, 3, 4, 5$. The superiority of the Roy model over the conventional pattern-mixture model is seen in the two-class model having better log-likelihood with fewer parameters. In terms of BIC, the four-class model is preferable.

The “misclassification” referred to in the Roy (2003) quote above is clearly evident in the STAR*D example. There is little agreement in the cross-classification of subjects between using the six pattern-mixture dropout patterns and using Roy four-class latent dropout classes. As will be shown, this is likely due to the latent dropout classes being influenced also by trajectory types.

In line with conventional pattern-mixture modeling, the Roy latent dropout modeling is primarily focused on the mixture over the latent classes: “While the class-specific estimates are informative, they are not of primary interest” (Roy, 2003, p. 834). The resulting depression mean curve estimated by Roy latent dropout modeling largely overlaps that of pattern-mixture modeling given in Figure 3 and is not shown. The curves of Figure 3, however, do not reveal whether subgroups of subjects show different results under different NMAR models and under MAR.

Instead of mixing over the four classes of the Roy latent dropout model, it is of interest to consider their interpretation in terms of antidepressant response and compare them to that of the four-class

<table>
<thead>
<tr>
<th>Model</th>
<th>Log-likelihood</th>
<th>Number of parameters</th>
<th>BIC</th>
</tr>
</thead>
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<tr>
<td>Pattern-mixture</td>
<td>-44946</td>
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<td>90117</td>
</tr>
<tr>
<td>Roy 2c</td>
<td>-44871</td>
<td>24</td>
<td>89942</td>
</tr>
<tr>
<td>Roy 3c</td>
<td>-44777</td>
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</tr>
<tr>
<td>Roy 4c</td>
<td>-44728</td>
<td>42</td>
<td>89806</td>
</tr>
<tr>
<td>Roy 5c</td>
<td>-44698</td>
<td>51</td>
<td>89820</td>
</tr>
</tbody>
</table>

Note. The best model is shown in bold. BIC = Bayesian information criterion.
MAR growth mixture model of Figure 5. The four estimated mean
depression curves are shown in Figure 7. The trajectory shapes,
and therefore the interpretations of the latent classes, are in line
with Figure 5. For the Roy model, only 43% of the subjects are
estimated as responding, with as many as 28% nonresponders and
18% showing a U-shaped curve of transient improvement. In
summary, the Roy NMAR model gives a considerably worse
assessment of the drug efficiency than the four-class MAR model.

**Beunckens Selection Modeling With Latent Subgroups of Subjects**

Beunckens et al. (2008) introduced a model that combines
selection modeling features with shared-parameter modeling fea-
tures. The model has selection features in that it uses discrete-time
survival dropout indicators as dependent variables influenced by
the random effects of the outcome process for \( y \) in line with Wu
and Carroll (1988). The model has shared-parameter modeling
features in that both the survival dropout indicators and the de-
pression outcomes are influenced by a latent class variable and
random effects.

A special case of the model can be specified in line with
Beunckens et al. (2008, Equation 7), where the survival dropout
indicators are influenced by both latent class and the random
intercept \( \eta_0 \):

\[
y_{it} | c_i = k = \eta_0 + \eta_{1i} \left( a_i - \bar{a} \right) + \eta_{2i} \left( a_i - \bar{a} \right)^2 + \varepsilon_{it}, \quad (10)
\]

\[
\eta_0 | c_i = k = \alpha_{0k} + \xi_{0i}, \quad (11)
\]

\[
\eta_{1i} | c_i = k = \alpha_{1k} + \xi_{1i}, \quad (12)
\]

\[
\eta_{2i} | c_i = k = \alpha_{2k} + \xi_{2i}, \quad (13)
\]

\[
\log \left( \frac{P(d_{it} = 1 | c_i = k, \eta_{0k})}{P(d_{it} = 0 | c_i = k, \eta_{0k})} \right) | c_i = k = \alpha_i + \beta_{1i} \left( a_i - \bar{a} \right) + \beta_{2i} \left( a_i - \bar{a} \right)^2 + \beta_3 \eta_{0i}, \quad (14)
\]

where in Equation 14 the dependence of dropout on latent class
in the first three terms is formulated as a quadratic latent class growth
model that reduces the number of parameters relative to estimating
free parameters for each class and time point. As before, the \( d \)
variables are scored as discrete-time survival indicators, obtaining
the value 0 for periods before the dropout event occurs, 1 at the
time the dropout occurs, and missing for the periods after the event
occurs (Mutheñ & Masyn, 2005). The model is shown in diagram
form in Figure 8.

The results of fitting one to five classes are shown in Table 3.
The one-class model is in line with Wu and Carroll (1988). The
four-class model has the best BIC. For comparison the results for
the Diggle–Kenward model are also given. It has a better BIC than
the one-class Beunckens model but worse BIC than the four-class
Beunckens model.

The estimated mean trajectories for the four-class Beunckens
model are shown in Figure 9. The low class of responding subjects
is estimated as 35%, whereas the high class is estimated as 25%
and the U-shaped class is estimated as 19%.

The Beunckens model is related to mixed-effects hybrid mod-
eling proposed by Yuan and Little (2009). In both cases discrete-
time survival is predicted by random effects (growth factors).
Whereas Beunckens lets the random-effect means vary over latent
classes, Yuan–Little lets the means vary over categories defined by
dropout time. Because of the latent versus observed categories
distinction, the Yuan–Little approach relates to the Beunckens
approach much like pattern-mixture modeling relates to Roy mod-
eling. The Yuan–Little modeling can be handled as in Figure 8,
with an added covariate representing dropout time that influences
the growth factors.

![Figure 7. Four-class Roy latent dropout model. QIDS = Quick Inventory of Depressive Symptoms–Clinician Rated.](image-url)
Extensions of NMAR Models

This section explores the STAR*D data with two new NMAR models. First, the Roy pattern-mixture model is expanded to include a second latent class variable. Next, the Diggle–Kenward selection model is generalized to include latent subgroups of subjects.

Pattern-Mixture Modeling: Muthén–Roy Modeling With Latent Subgroups of Subjects

For both conventional pattern-mixture modeling and Roy latent dropout modeling, the intention is to mix the parameter estimates over the patterns or classes to obtain an overall estimated growth curve. This mixing may, however, hide substantively interesting trajectory classes. Furthermore, the Roy approach forms classes based not only on the relationship between dropout and outcomes but also on the development of the outcomes over time. This may confound dropout classes with trajectory classes.

To alleviate these concerns, a new type of pattern-mixture model is introduced here, with a generalization that allows for two distinct latent class variables: one related to dropout and another related to the outcome trajectories. The former latent class variable summarizes trajectories of the depression outcome \(y_t\). The two latent class membership relationships, for \(t = 1, \ldots, T\) are as follows:

\[
\begin{align*}
\eta_{1t} | cd_i = 1, cy_i = 1, d_{ij} & = \eta_{01} + \eta_{1i} (a_i - \bar{a}) + \eta_{2i} (a_i - \bar{a})^2 + \epsilon_{1i}, \\
\eta_{0i} | cd_i = 1, cy_i = 1, d_{ij} & = \alpha_{00} + \xi_{0i}, \\
\eta_{1i} | cd_i = 1, cy_i = 1, d_{ij} & = \alpha_{10} + \xi_{1i}, \\
\eta_{2i} | cd_i = 1, cy_i = 1, d_{ij} & = \alpha_{20} + \xi_{2i}.
\end{align*}
\]

The two latent class membership relationships,

\[
P(cd_i = k | d_{ij}, \ldots, d_{Tj}) = \frac{e^{\gamma_{0k} + \sum_{l=1}^{K} \gamma_{lk} d_{ij}}}{\sum_k e^{\gamma_{0k} + \sum_{l=1}^{K} \gamma_{lk} d_{ij}},}
\]

\[
P(cd_i = k, cy_i = l | d_{ij}, \ldots, d_{Tj}) = \frac{e^{\gamma_{0kl} + \sum_{l=1}^{K} \gamma_{lkl} d_{ij}}}{\sum_k e^{\gamma_{0kl} + \sum_{l=1}^{K} \gamma_{lkl} d_{ij}}}.
\]

Note. The best model is shown in bold. BIC = Bayesian information criterion.
tendency to stay in the study. The legends give the class percentages for the different curves.

It is interesting to compare the estimated dropout curves of Figure 11 to the Figure 1 observed means before dropout denoted by triangles. The dropout curves for Figures 11A and 11C appear to reflect the observed means for subjects moved to the next level seen in Figure 1B. The U-shaped dropout curves for Figures 11B and 11D appear to reflect the observed means for subjects moved to follow-up seen in Figure 1C. These relationships are explored in a later section.

Figure 11B shows two classes with similar development of decreasing depression scores up to Week 6, where both curves are close to the level deemed as “remittance.” The 14.8% Class 2 subjects, however, show a U-shaped curve with a substantially worsening depression level by Week 12, whereas the 24% Class 6 subjects respond. It is of substantive interest to further explore the different characteristics of subjects in these two classes. Class 2 subjects may be prematurely moved to the follow-up phase.

A second U-shaped curve is found in Class 4 with 4.5% of the subjects, although not dipping as low as for Class 2. A second class, Class 8 with 8%, shows response, adding to a total 32% showing response with this model. The corresponding percentage for the U-shaped class of the four-class Roy model is similar at 18%, whereas the response class percentage of 43% is somewhat higher. Choosing between models is discussed in a later section.

Selection Modeling: Diggle–Kenward Modeling With Latent Subgroups of Subjects

The Diggle–Kenward model may be contrasted with the Beunckens model. In the former, the survival dropout indicators are influenced directly by the depression outcomes. In the one-class case, this gives a better BIC than having survival be influenced by random effects. The use of multiple classes, however,
makes the Beunckens model have a better BIC than Diggle–Kenward. For these reasons, the Diggle–Kenward model is here extended to a mixture model specified as follows:

\[ y_{ti} | \alpha = \eta_{0i} + \eta_{1i} (a_i - \bar{a}) + \eta_{2i} (a_i - \bar{a})^2 + \epsilon_{ti}, \quad (22) \]

\[ \eta_{0i} | \alpha = \alpha_{0i} + \xi_{0i}, \quad (23) \]

\[ \eta_{1i} | \alpha = \alpha_{1i} + \xi_{1i}, \quad (24) \]

\[ \eta_{2i} | \alpha = \alpha_{2i} + \xi_{2i}, \quad (25) \]

\[ \log \left[ \frac{P(d_i = 1 | y_{ti}, y_{i-1}, \ldots)}{P(d_i = 0 | y_{ti}, y_{i-1}, \ldots)} \right] |_{\alpha} = \alpha_{0i} + \beta_{1i} y_{ti} + \beta_{2i} y_{i-1}, \quad (26) \]

Alternatively, a quadratic latent class growth model can be specified for the \( \alpha_{0i} \) coefficients in line with Equation 14. The logistic regression slopes \( \beta \) of Equation 26 are here allowed to vary across the latent classes. This is important because subjects in high-trajectory classes tend to drop out due to high depression values, whereas subjects in the low class tend to drop out due to low depression values.

To provide further generality, we also allowed the \( \beta \) slopes to vary across time. For example, a subject’s dropout probability may be less influenced by the depression score early in the study, whereas later failure to reduce depression may have greater influence on dropout. The model is shown in diagram form in Figure 10B.

Table 4
Comparing Maximum Likelihood Results for Roy and Muthén–Roy Mixture Models

<table>
<thead>
<tr>
<th>Model</th>
<th>Log-likelihood</th>
<th>Number of parameters</th>
<th>BIC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roy 4c (1cy, 4cd)</td>
<td>-44728</td>
<td>42</td>
<td>89806</td>
</tr>
<tr>
<td>Muthén–Roy (2cy, 2cd)</td>
<td>-44743</td>
<td>30</td>
<td>89736</td>
</tr>
<tr>
<td>Muthén–Roy (2cy, 3cd)</td>
<td>-44702</td>
<td>41</td>
<td>89744</td>
</tr>
<tr>
<td>Muthén–Roy (3cy, 2cd)</td>
<td>-44654</td>
<td>52</td>
<td>89740</td>
</tr>
<tr>
<td>Muthén–Roy (3cy, 3cd)</td>
<td>-44696</td>
<td>37</td>
<td>89699</td>
</tr>
<tr>
<td>Muthén–Roy (4cy, 2cd)</td>
<td>-44647</td>
<td>51</td>
<td>89717</td>
</tr>
<tr>
<td>Muthén–Roy (4cy, 3cd)</td>
<td>-44662</td>
<td>34</td>
<td>89689</td>
</tr>
</tbody>
</table>

Note. The best model is shown in bold. BIC = Bayesian information criterion.

Figure 11. Muthén–Roy mixture model with four trajectory classes and two dropout classes (curves marked with triangles correspond to a higher tendency to drop out): (A) the Class 1 and Class 5 pair of curves; (B) the Class 2 and Class 6 pair of curves; (C) the Class 3 and Class 7 pair of curves; (D) the Class 4 and Class 8 pair of curves. QIDS = Quick Inventory of Depressive Symptoms–Clinician Rated.
Table 5 shows the results of fitting a series of Diggle–Kenward selection mixture models with four classes as for the Beunckens model. For comparison, the conventional one-class Diggle–Kenward model is also presented. The four-class Model 1 specifies class- and time-invariant $\beta$ slopes in Equation 26 as well as class-invariant $\alpha_i$ values. The four-class Model 2 allows class-varying $\alpha_i$ and class-varying $\beta$, where the class variation in $\alpha_i$ is specified as a quadratic function as in Equation 14. The four-class Model 3 is as the four-class Model 2 but also allows $\beta$ variation across time. It is clear from both BIC and likelihood-ratio chi-square testing that the four-class Model 3 is preferable. In view of the BIC, this model is also preferable to the four-class Beunckens model of Table 3.

The estimated mean curves for the four-class Model 3 are shown in Figure 12. The low class of subjects who respond is estimated as 45%, the high class of nonresponders is estimated as 18%, and the U-shaped class is estimated as 6%. These estimates lie in between those obtained with MAR on the one hand and those of Muthén–Roy and Beunckens on the other hand.

**Comparing Models**

**Summary of Percentages**

This section summarizes the results for the preferred models: the four-class model in the MAR family, the Muthén–Roy 4c, 2c model in the pattern-mixture family, and the Diggle–Kenward four-class Model 3 in the selection family. Table 6 gives the model-estimated percentages for the high class, the U-shaped class, and the low class for these three models.

It is also useful to consider model-estimated results presented in the traditional form of antidepressant trials. Traditionally, remission is defined as an endpoint depression score less than a certain cut-point, in this case a Week 12 QIDS score of $\leq 5$. Also, drug response is defined as a drop in the depression score of at least 50% from baseline to Week 12. Table 6 also includes these percentages for the three models, as well as for the traditional one-class MAR model.

It is clear from Table 6 that the models have a wide range of estimates for the percentage in the three latent classes. The four-class MAR model has a high response rate of 55%, with a total of only 18% in the failing high and U-shaped classes. This gives a much more positive view of the antidepressant than the Muthén–Roy model’s 32% responders and 29% in the failing high and U-shaped classes.

For all the models, the low class percentage is closer to the response percentage than the remission percentage. Although the mean of the low class at Week 12 is below the $\leq 5$ cutoff, not all subjects in the class are. Instead, the trajectory shape determines the class membership.

**Choosing Between Models**

Choosing between the MAR, pattern-mixture, and selection models is difficult given that the three model types have different likelihood and BIC metrics. The different metrics are due to the models having different sets of dependent variables. The log-likelihoods of pattern-mixture, Roy, and Muthén–Roy models are comparable. Likewise, the selection models of Diggle–Kenward and Beunckens have comparable log-likelihoods. Comparing log-likelihoods between models not belonging to the same family, however, is not informative. Nor are the log-likelihoods for either
Table 6

Summary of Key Model-Estimated Percentages for Latent Class, Remission, and Response

<table>
<thead>
<tr>
<th>Model</th>
<th>High class</th>
<th>U-shaped class</th>
<th>Low class</th>
<th>Remission (≥5)</th>
<th>Response (≥50% drop)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Missing at random 4c</td>
<td>15</td>
<td>3</td>
<td>55</td>
<td>34</td>
<td>53</td>
</tr>
<tr>
<td>Muthén–Roy (4c, 2c)</td>
<td>14</td>
<td>15</td>
<td>32</td>
<td>22</td>
<td>34</td>
</tr>
<tr>
<td>Diggle–Kenward 4c</td>
<td>18</td>
<td>6</td>
<td>45</td>
<td>26</td>
<td>45</td>
</tr>
<tr>
<td>Missing at random 1c</td>
<td></td>
<td></td>
<td></td>
<td>27</td>
<td>49</td>
</tr>
</tbody>
</table>

NMAR family comparable to MAR models, a fact that is not always made clear in the NMAR literature. For example, it is not correct to view the MAR mixture model as a special case of the Roy model where there is no influence of dropout indicators on latent class membership, that is, \( \gamma_{ik} = 0 \) in Equation 9. This is because the MAR model allows for dropout and the \( y \) outcome to be related in that observed \( y \) values are allowed to influence dropout (see, e.g., Demirtas & Schafer, 2003).

The question arises as to which analysis strategy a researcher should take with dropout. It is suggested here that a first step is to find the best model via BIC within each of the three families of models: MAR (including both single- and multiple-class models), pattern-mixture (including Roy and Muthén–Roy modeling), and selection (single- and multiple-class models). If results from the three approaches all agree, then the MAR results are supported, and a researcher can present the MAR results with the additional information that NMAR explorations do not contradict the findings. If pattern-mixture and selection modeling agree, but the MAR results disagree in substantively important ways, it seems reasonable to present both the MAR and NMAR results and raise the possibility that the NMAR results may be more trustworthy. If results from all three approaches disagree, there is no statistical basis for preferring the results of any of the models. Instead, the range of results need to be reported as in Table 6.

In some exceptional cases, however, the models can be compared in terms of how they relate to auxiliary information about the reasons for dropout. Such information is fortunately available in the STAR*D data. This is explored next.

Adding Auxiliary Information

The STAR*D data have useful auxiliary information in the form of the subject’s ending status in the 12-week Level 1 part of the trial. As mentioned in the introduction, STAR*D distinguished between three end categories: Subjects were moved to the next level if the medication was not completely effective or not tolerated; subjects were moved to follow-up if showing remission; or subjects exited the study for unknown reasons. With a missing data category added, this gives a four-category nominal variable \( u \), say, standing for ultimate, or distal, outcome. The three competing models—MAR, Muthén–Roy, and mixture Diggle–Kenward—can be augmented by the \( u \) outcome, where the added parameters are the three \( u \) probabilities varying across the latent classes of those models. The \( u \) variable is useful for NMAR modeling because it carries more information than the observed \( y \) outcome given that it also relates to side effects and subject preferences. The ability of the original model to capture nonignorable missingness can be assessed by studying the congruence in the latent class formation between including and not including the \( u \) variable in the model.

The Muthén–Roy model can be extended to allow \( u \) to be influenced not only by the two latent class variables \( c d \) and \( c y \) but also by the dropout indicators \( d \). For \( r = 1, 2, \ldots, R (R = 4) \),

\[
P(u_i = r | c d_i = k, c y_i = l, d_{i1}, \ldots, d_{iR}) = \frac{e^{\gamma_{ru} + \sum_{k} \gamma_{rk} d_k}}{\sum_{r'} e^{\gamma_{ru'} + \sum_{k} \gamma_{rk'} d_k}}
\]

Figure 13 shows the extended Muthén–Roy model in diagram form. In the extended model, the relationship between latent class membership and the end categories provides a predictive validity check of the latent classes.

Figure 14 shows the estimated mean curves for the MAR and mixture Diggle–Kenward models extended to include \( u \). Figure 15 shows the estimated mean curves for the extended Muthén–Roy model. Unlike for Figure 11, the eight curves are shown in a single graph. The specification in Equation 27 was used for Muthén–Roy, where including the \( d \) as covariates influencing \( u \) improved the BIC but had little effect on the parameter estimates. The extended MAR model retains the trajectory shapes of the original latent classes, but it is seen that it obtains a lower percentage in the low class than in the original MAR model, 42% compared with 55%. The extended mixture Diggle–Kenward model also obtains a re-
duced percentage in the low class, 37% compared with 45%. The high class is reduced from 18% to 15%. The extended mixture Diggle–Kenward model does not, however, retain the U-shaped class of the original Diggle–Kenward model. The extended Muthén–Roy model largely retains the trajectory shapes of the original model. The low class percentage remains unchanged at 32%, and the high class percentage changes only from 14% to 13%. The U-shaped class is now more clearly accentuated and distinguished as the only class that shows a substantial temporary improvement, with an outcome well below 5, and subsequent worsening. The class percentage is changed from 15% to 9%. All in all, the Muthén–Roy model appears as the model most congruent with the u outcome.

The Muthén–Roy plot shows an interesting phenomenon related to the U-shaped class and the low class. Starting out the same as the low class, the U-shaped class has the higher dropout tendency. This is because many subjects in the 9% U-shaped class have a score of ≤5 and are likely to be moved to follow-up. The U-shaped class, however, is characterized by a temporary improvement and later worsening. The low class estimate of 37% in the extended mixture Diggle–Kenward model may be biased upward because it does not allow for a portion of those subjects following U-shaped trajectories. The existence of such subjects in the data is demonstrated in Figure 16, showing observed trajectories for subjects classified into the U-shaped class by the extended Muthén–Roy model. In this sense, the Muthén–Roy model appears more flexible than the mixture Diggle–Kenward model in this application.

Table 7 considers the predictive aspects of the latent classes. It shows the estimated probabilities for the four categories of the

Figure 14. (A) Estimated means under the missing-at-random model extended to include an ultimate outcome. (B) Estimated means under the mixture Diggle–Kenward model extended to include an ultimate outcome.
given latent class membership for the extended Muthe´n–Roy model. Subjects in the low class have a high probability of ending up in the follow-up category corresponding to remission. Subjects in the high class are likely to be moved to the next level with treatment by other antidepressants but have a sizable probability of exiting the study. Subjects in the U-shaped class are likely to be moved to follow-up but also have a sizable probability of exiting the study. The high percentage (62%) moved to follow-up in this class of rapid but transient improvement points to a problem of counting these individuals as remitters.

Figure 15. Estimated means under the Muthe´n–Roy model extended to include an ultimate outcome. QIDS = Quick Inventory of Depressive Symptoms–Clinician Rated.

Conclusions

It is of interest to see whether the growth mixture model results under MAR are trustworthy given that missingness may be NMAR. Applying a series of NMAR models in a sensitivity analysis provides useful information regarding this question. On the whole, the MAR mixture model results, the Muthe´n–Roy mixture model results, and the mixture Diggle–Kenward selection model results for the STAR*D data have similarities in terms of

Figure 16. Observed individual trajectories for subjects classified into the U-shaped class under the extended Muthe´n–Roy model. QIDS = Quick Inventory of Depressive Symptoms–Clinician Rated.
trajectory shapes. The models do differ, however, in the latent trajectory class percentages, which impacts the assessment of the drug effectiveness. The conventional MAR four-class model estimates that 55% of the subjects are in the response class with 18% in failing classes, whereas the extended Muthén–Roy model gives the response estimate of 32% with 29% in failing classes. Follow-up analysis with the Level 1 ultimate outcome classification in the STAR*D trial lends credence to the Muthén–Roy estimate. Furthermore, the Muthén–Roy finding of a 9% U-shaped class of subjects who may be prematurely deemed as remitting is of clinical importance in that it suggests a transient improvement.

The different models have quite different computational demands in the maximum likelihood estimation. The MAR mixture model has rather light computations, the Muthén–Roy model has moderately heavy computations, and the mixture Diggle–Kenward model has very heavy computations. The expectation–maximization computations of the mixture Diggle–Kenward model involve numerical integration over the unobserved outcomes, which is handled via Monte Carlo integration. Combined with using many random starting values to avoid local maxima, this leads to quite slow computations. The Beunckens model is lighter in this regard, given that integration needs to be done only with respect to the random effects. Scripts for the analyses are available at http://www.statmodel.com/examples/penn.shtml#stard via the Mplus program (Muthén & Muthén, 2010).

The modeling can also be extended in several ways within the general latent variable framework handled in Mplus. Covariates can predict the latent class variables as well as random effects within class and outcomes directly. Outcomes can be binary, ordered polytomous, censored-normal, and counts. Multilevel data can be handled with Level 2 latent class variables.

In addition to modeling dropout, the general latent variable framework can handle modeling of the binary missing data indicators m so that intermittent missingness is included. For example, it is possible to apply a two-part (semicontinuous) growth mixture model extending the work of Olsen and Schafer (2001). The model can be expressed as two parallel processes, one for the outcomes and one for the binary missing data indicators. At a given time point, the outcome is missing or not depending on the missing data indicator. The two processes have growth models with latent class variables and random effects that are correlated across the processes. Such a model is shown in diagram form in Figure 17.

In the current STAR*D example, a large sample size is available for analysis (N = 4,041). Many data sets in psychology are of considerably smaller size. Fortunately, a large sample size is not a prerequisite for NMAR analysis. For example, the schizophrenia example in Demirtas and Schafer (2003) with 437 participants was successfully reanalyzed with two-class pattern-mixture and selection models. It is likely that smaller samples can also be used as long as the trajectory classes are sufficiently well separated. To determine the performance of the analyses, simulation studies can be carried out in Mplus, where different types of NMAR missing data can be generated.

References


Table 7

<table>
<thead>
<tr>
<th>Latent class</th>
<th>Next level</th>
<th>Follow-up</th>
<th>Exit</th>
<th>Missing</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low</td>
<td>.00</td>
<td>.94</td>
<td>.04</td>
<td>.02</td>
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<tr>
<td>High</td>
<td>.63</td>
<td>.00</td>
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<td>U-shaped</td>
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<td>.62</td>
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