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At the frontiers of modeling intensive longitudinal data: Dynamic structural
equation models for the affective measurements from the COGITO study

REVISED VERSION

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Abstract

With the growing popularity of intensive longitudinal research, the modeling techniques and software options for such data are also expanding rapidly. Here we use dynamic multilevel modeling, as it is incorporated in the new dynamic structural equation modeling (DSEM) toolbox in Mplus, to analyze the affective data from the COGITO study. These data consist of two samples of over one hundred individuals each who were measured for about one hundred days. We use composite scores of positive and negative affect and apply a multilevel vector autoregressive model to allow for individual differences in means, autoregressions and cross-lagged effects. Then we extend the model to include random residual variances and covariance, and finally we investigate whether prior depression affects later depression scores through the random effects of the daily diary measures. We end with discussing several urgent—but mostly unresolved—issues in the area of dynamic multilevel modeling.

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The COGITO study, which took place a decade ago, is an impressive project that reflects an admirable determination on part of its researchers as well as the participants. It consists of a younger and an older sample of over 100 individuals each, who visited the laboratory on about 100 days to perform a battery of cognitive tests and fill out self-report questionnaires. This endeavor is all the more impressive if one realizes that at the time, gathering intensive longitudinal data was not only cumbersome, but it was also considered unnecessary by many, because short-term, within-person fluctuations were assumed to reflect mere noise. Since then, however, the tide has turned: first, technological developments like smart phones and wearable devices have led to new forms of data collection—such as ambulatory assessments, experience sampling, ecological momentary assessments, and electronic daily diaries (Conner, Tennen, Fleeson, & Feldman Barrett, 2009; Trull & Ebner-Priemer, 2013)—that have placed intensive longitudinal data within reach of mainstream psychology; and second, the growing body of research made possible by these innovations now forms a convincing testimony of the meaningfulness of short-term, within-person fluctuations.

While intensive longitudinal research like the COGITO study has many

favorable features, one of its most valuable properties is that it provides a unique opportunity to study processes as they unfold over time (Hamaker & Wichers, 2017). To investigate the underlying dynamics of intensive longitudinal data, researchers have been borrowing techniques from other disciplines like econometrics, physics and engineering, where they have a long history of modeling processes over time (e.g., Bisconti, Bergeman, & Boker, 2004; Chow, Nesselrode, Shifren, & McArdle, 2004; Chow, Ram, Boker, Fujita, & Clore, 2005; Hamaker, Dolan, & Molenaar, 2002, 2003; Molenaar, 1985; Molenaar, 1987; Ram et al., 2005; Rovine & Walls, 2006; Sadler, Ethier, Gunn, Duong, & Woody, 2009). However, in contrast to the practice in many of these alternative disciplines where data typically come from a single case, a fundamental challenge in psychology and other social sciences is how to combine and compare the intensive longitudinal data of multiple individuals. We can distinguish between two approaches in this respect (see S. Liu, 2017, for a first comparison between these two).

In the *bottom-up approach*, sometimes referred to as replicated time series analyses, the data are first analyzed per person, and subsequently similarities between the dynamics of different individuals are sought. This can be done by the researchers themselves through constraining parameters across individuals (cf. Hamaker et al., 2003), for instance when using software like the R-packages *OpenMx* (Boker et al., 2011) and *dynR* (Ou, Hunter, & Chow, under review). Alternatively, the R-package *Group Iterative Multiple Model Estimation* (GIMME; Gates & Molenaar, 2012; Beltz, Wright, Sprague, & Molenaar, 2016) can be used to automatically search for such similarities. This bottom-up approach can be considered a purely idiographic research form that allows for a maximum degree of

idiosyncracies in the results.

In contrast, the *top-down approach*, also referred to as dynamic multilevel modeling, is based on choosing a particular time series model or differential equation to describe the variability within an individual at level 1, while allowing for quantitative differences at level 2 in the parameters that govern these dynamics. This approach can be considered as somewhere in between idiographic and nomothetic research (cf., Conner et al., 2009): While it is assumed that the functional form of the level 1 model is the same for individuals, there is ample room for quantitative differences between individuals in the parameters of this function. Researchers have been applying this approach using Bayesian software like *JAGS* (Plummer, 2003) and *WinBUGS* (Spiegelhalter, Thomas, Best, & Lunn, 2003; e.g., Wang, Hamaker, & Bergman, 2012), but there are also specialized programs that were developed for this purpose. These include the *Bayesian Ornstein-Uhlenbeck Model* (BOUM) toolbox package (Oravecz, Tuerlinckx, & Vandekerckhove, 2016), the R-package *mlVAR* (Epskamp, Deserno, & Bringmann, 2017), and the R-package *ctsem* (Driver, Oud, & Voelke, 2017), which in turn uses either *OpenMx* (Boker et al., 2011) or *Stan* (Stan Development Team, 2017).

In the current study we take a dynamic multilevel modeling approach to analyze the affective ratings obtained as part of the COGITO study. Specifically, we will show how various modeling innovations that have been proposed and developed in recent years—including standardization of cross-lagged parameters in dynamic multilevel models, random residual variances, and indirect effects through random effects—can now be easily combined and extended when using the new *dynamic structural equation modeling* (DSEM) module that is implemented in Mplus (cf.

Asparouhov, Hamaker, & Muthén, 2017a, 2017b). In doing so, we aim to illustrate the unique opportunities offered by dynamic multilevel modeling for studying the dynamics of processes, while also outlining the many unresolved issues in this emerging field.

This paper is organized as follows. First, we explain how intensive longitudinal data can be decomposed into different sources of variance, which is fundamental to dynamic multilevel modeling, and we illustrate this with the COGITO data. Second, we discuss some of the basics of DSEM in Mplus, which are essential for the dynamic multilevel models we use in the current study. This is followed by three analyses on the COGITO affective data, consisting of increasingly more advanced dynamic multilevel models, that is: a) a bivariate multilevel cross-lagged model that allows for individual differences in means, autoregressive relationships, and cross-lagged relationships; b) an extension of this model with random innovation variances and covariance, to account for individual differences in these model features; and c) an extension that includes a predictor at level 2, which has indirect effects through the random effects of the affect dynamics on an outcome variable at level 2. In these analyses we make the following assumptions: a) the data are normally distributed, both within persons and between persons; b) there are no trends or cycles over time in these data; and c) missing data are missing at random. Clearly, these are strong assumptions that should be further investigated in practice; however, practical solutions in case these assumptions are violated are not always straight forward and/or readily available. We discuss these and other urgent—yet unresolved—issues that come up while analyzing the COGITO data at the end of this paper.

Total, cross-sectional, within-person, and between-person
variability

There is quite a large body of literature regarding the actual meaningfulness of cross-sectional research for gaining knowledge about processes that operate within individuals (e.g., Borsboom, Mellenbergh, & Van Heerden, 2003; Cattell, 1952; Grice, 2004; Hamaker, 2012; Hamaker, Schuurman, & Zijlmans, 2017; Lamiell, 1998; Molenaar, 2004; Molenaar, Huizenga, & Nesselroade, 2003; Nesselroade, 2002; Schmitz & Skinner, 1993; Voelkle, Brose, Schmiedek, & Lindenberger, 2014). This topic is already complex in itself, but the discussion is further complicated by the fact that researchers sometimes use the same terms to refer to different phenomena. Therefore, we begin by briefly explaining our terminology and how this relates to the conventions in different strands of literature. Once this is in place, we decompose the affective measurements from the COGITO study.

Terminology

While the terms *within-person* and *intraindividual* variability unambiguously refer to the variability *within a person over time and/or situations*, their linguistic counterparts *between-person* and *interindividual* variability have been used to refer to two distinct forms of variation: At times, they are used to refer to *stable, trait-like variation between persons* (Hamaker, Nesselroade, & Molenaar, 2007; Wang & Maxwell, 2015), and at other times they are used to refer to *cross-sectional variation*, that is, the variability across persons at a single occasion (Borsboom et al., 2003; Hamaker, Dolan, & Molenaar, 2005; Molenaar, 2004; Voelkle et al., 2014). This ambiguous usage of the terms *between-person* and *interindividual* may have led

some researchers to erroneously conclude that there is no difference between trait-like variation and cross-sectional variation, and as a result, cross-sectional variation may easily be mistaken as the counterpart of intraindividual or within-person variation.

In the current paper, we will use these terms in accordance to the multilevel literature, such that between-person and interindividual are the complement of within-person and intraindividual. This implies that cross-sectional variability is the result of both within-person and between-person variability (cf. Hamaker et al., 2017; Hamaker et al., 2007; Schmitz, 2000). Finally, we will use the term *total variability* to refer to the variability both across individuals and across time points. The latter is thus also the result of within-person and between-person variability, but in contrast to cross-sectional variability, which is restricted to a single time point, the total variability can also contain variability over time.

Decomposing the COGITO affective data

We consider within, between and total variability using the composite scores obtained from the positive affect negative affect schedule (PANAS; Watson, Clark, & Tellegen, 1988), which the COGITO participants filled out at each measurement occasion (Brose, Voelkle, Lövdén, Lindenberger, & Schmiedek, 2015). The PANAS consists of ten items that measure positive affect (PA) and ten items that measure negative affect (NA). We analyze the data of the younger sample (aged 20-31), consisting of 101 individuals, and the older sample (aged 65-80), which consists of 103 individuals, separately.¹

First, we estimate the total variances for PA and NA and the corresponding total correlation based on all the data in the sample, both across persons and time.

Second, the within-person and between-person results are obtained using a basic multivariate multilevel model (sometimes referred to as the empty model, as it does not include any predictors): It decomposes the total variance into two parts, that is, the between part, which is formed by the within-person means (sometimes referred to as cluster or group means), and the within-part, which are formed by the within-person fluctuations over time around the within-person means. Let PA_{it} and NA_{it} be the PA and NA scores of individual i at time t . The decomposition into the within-person and between-person parts is

$$PA_{it} = \mu_{PA,i} + PA_{it}^{(W)} \quad \text{and} \quad NA_{it} = \mu_{NA,i} + NA_{it}^{(W)},$$

or in matrix notation

$$\begin{bmatrix} PA_{it} \\ NA_{it} \end{bmatrix} = \begin{bmatrix} \mu_{PA,i} \\ \mu_{NA,i} \end{bmatrix} + \begin{bmatrix} PA_{it}^{(W)} \\ NA_{it}^{(W)} \end{bmatrix}, \quad (1)$$

where the μ 's are the within-person means that form the between-person part of the model, and $PA_{it}^{(W)}$ and $NA_{it}^{(W)}$ represent the temporal deviations of individual i at occasion t from these within-person means.

In Figure 1, the variance estimates are plotted along with bars for the standard errors. The intraclass correlation (ICC) for each variable in each group is also reported: It is computed as the ratio of between-person variance to total variance, where the latter is the sum of within-person and between-person variance. Hence, the ICC indicates the proportion of the total variance that is accounted for by stable, trait-like between-person differences. Figure 1 shows that: a) the between-person variance is larger than the within-person variance for both PA and NA in both groups (ICCs lie between .62 and .89); b) the variance of PA is larger than that of NA in both groups and this is true for the total, the between and the

within variances; and c) the older sample is characterized by larger ICCs, and also by larger differences between the variability in PA and NA than the younger sample.

Insert Figure 1 about here

The correlations between PA and NA also differed across the between-person and within-person levels. At the between-person level the correlation between PA and NA did not differ significantly from zero in either sample, whereas at the within-person level there was a negative correlation in both samples ($\hat{\rho} = .19$, $SE=.01$, $p < .001$ in the younger sample, and $\hat{\rho} = .19$, $SE=.01$, $p < .001$ in the older sample). These results can be understood in the following way (see also Brose, Voelkle, et al., 2015). The traits PA and NA, which are captured by the between-person part of the model, are not correlated in these populations, which implies that sampling an individual who is high on one of these traits and low on the other is about equally likely as sampling an individual who is high on both traits, or low on both traits. In contrast, it is not that common to experience both elevated levels of PA and NA at the same time, because repeated measures of PA and NA are typically negatively correlated within a person. In the current dataset, the within-person variability refers to day-to-day fluctuations, rather than moment-to-moment fluctuations; therefore, the correlation of -.19 in both samples suggests that individuals tend to experience good days with elevated PA and decreased NA, and bad days with elevated NA and decreased PA instead, although this pattern is not as strong as in momentary measurements (when individuals are asked how they are feeling right now).

In sum, these results show that there are marked differences between the within-person and the between-person relationships, and that neither is represented well by the results for the total. This also confirms the concern that has been expressed by many researchers before: Cross-sectional results are a mix of within-person and between-person relationships, and may not represent either very well (cf. Brose, Schmiedek, & Lindenberger, 2013; Schmitz, 2000).² This decomposition of the total variance into a within-person and a between-person part is fundamental to dynamic multilevel modeling.

DSEM in a nutshell

To model the dynamics of these data, we make use of DSEM in Mplus. DSEM can be thought of as a combination of two time series techniques, that is: a) *state-space modeling*, which is a general framework used in estimating times series models (e.g., Durbin & Koopman, 2012; Harvey, 1989); and b) *dynamic factor analysis*, which is a factor analytic approach to time series data (e.g., Molenaar, 1985; Zhang, Hamaker, & Nesselroade, 2008). But where these time series techniques are traditionally concerned with $N = 1$ data (i.e., data from a single case; cf. Box & Jenkins, 1970; Chatfield, 2004; Hamilton, 1994; Kim & Nelson, 1999; Shumway & Stoffer, 2017), DSEM encompasses both $N = 1$ time series analysis and multilevel extensions of this (Asparouhov et al. (2017a); 2017b).

In this section we present some of the basics of DSEM that are relevant to the analyses of the COGITO affective data that we present afterwards. We begin by discussing the general model structure, consisting of a model at the within-person level, and a model at the between-person level. Subsequently, we discuss three key

issues, that is: the estimation used in DSEM, how missing data are handled, and how we can account for unequal intervals between observations.

The model

If we have longitudinal multilevel data, this implies that there is more than one person, dyad, or other unit, from which repeated measures have been obtained. If we want to analyze these data using DSEM in Mplus, the data should be in long format, which means that the repeated measures of a person should form separate rows in the data file, and there should be a cluster variable to indicate which rows belong to the same case.

Multilevel DSEM is based on decomposing the data into a within-person part and a between-person part, and modeling each of these parts with their own model. Let \mathbf{y}_{it} be the vector with p observed variables for individual i at time t . This is decomposed into a within-person vector with means $\boldsymbol{\mu}_i$, and a time-specific within-person vector with deviation from these mean $\mathbf{y}_{it}^{(W)}$, where the superscript (W) stands for ‘within’. Hence, the decomposition can be expressed as

$$\mathbf{y}_{it} = \boldsymbol{\mu}_i + \mathbf{y}_{it}^{(W)}, \quad (2)$$

similar to what was shown for the COGITO affect measures in Equation 1.

The temporal within-person deviations $\mathbf{y}_{it}^{(W)}$ are modeled with the *within-person level model*, which consists of a measurement equation that can relate observed variables to latent variables, and a structural equation in which latent variables can be related to each other. But in addition to such standard structural equation modeling properties, the within-person level model also allows for *lagged relationships* between variables, that is, regression paths between variables at

different time points. These lagged relationships can be between observed variables, between latent variables, or a combination of these. Moreover, factor loadings, regression coefficients and variances are allowed to be random, meaning that these parameters can take on different values for different individuals. These random effects thus allow for individual differences in for instance lagged relationships or residual variances, as we will show later on.

The random effects from the within-person level model and the random means from the decomposition automatically end up as latent variables in the *between-person level model*. Here they can be further modeled together with observed time-invariant (i.e., level 2 or between level) variables that have been included in the analysis. The between-person level model also consists of a measurement equation and a structural equation, allowing for the definition of factor models, path models, or a combination of these two based on all between-person variables.

Estimation in DSEM

DSEM as it is implemented in Mplus version 8, is based on Bayesian estimation. This makes it possible to have a large number of random effects, which would be intractable in a frequentist framework. Bayesian estimation is based on combining the likelihood of the data with prior distributions for the unknown model parameters to obtain posterior distributions for these unknown parameters (Gelman, Carlin, Stern, & Rubin, 2014; Lynch, 2007). Typically, estimation consists of an iterative process in which parameters are sampled from conditional distributions according to a Markov chain Monte Carlo (MCMC) procedure (Gelman et al., 2014). The priors can be used to incorporate prior knowledge or

subjective expectations into the model, but one can also specify flat, diffuse priors that contain little prior information; in the latter case, the results are asymptotically equivalent to maximum likelihood estimation. Mplus allows the user to specify the priors, but it also provides default priors that are diffuse so that the data dominate the results (Asparouhov & Muthén, 2010; Gelman et al., 2014); this is the option we will use here.

When using an MCMC algorithm to estimate parameters, we have to decide on the number of iterations. In Mplus we can either specify this number, or use the potential scale reduction (PSR) criterion, which is computed for each model parameter separately by dividing the *total variability across two chains* of the MCMC algorithm, by the *variance within a chain* (Asparouhov & Muthén, 2010; Gelman et al., 2014). This quantity should be very close to one, as the between-chain variance should be close to zero, such that the total variance across two chains becomes (almost) identical to the within-chain variance if enough iterations are used. Furthermore, it is considered good practice in Bayesian estimation to check the trace plots of each parameter, to see whether there are signs of non-convergence.

In the end, a burn-in period is discarded to erase the influence of starting values used by the MCMC algorithm. The remaining MCMC samples are considered an empirical approximation of the posterior distribution of the parameters. Point estimates are obtained by taking the mean or median for each parameter. In addition, credible intervals (CI) are obtained based on the posterior distributions through finding the lower and upper cut-off values of a particular interval (e.g., the 95% CI). Hence, these intervals are not based on the assumption

that each parameter has a normal or even symmetric distribution. Moreover, it is easy in Bayesian analysis to compute additional quantities of interest based on model parameters (e.g., indirect effects or standardized parameters), and obtain a CI for this, as the quantity can be computed at each iteration of the MCMC algorithm, thus providing a posterior distribution for the quantity.

Missing data

Missing data are very common in intensive longitudinal data; how we handle these may have serious consequences for the quality of our results. In Bayesian analyses, missing data are typically treated in the same way as random effects and model parameters, which implies that at each iteration of the MCMC algorithm, missing data are sampled from their conditional posterior. This conditional distribution takes the autocorrelation structure of the individual's data into account. For instance, if one is estimating a first-order autoregressive process and there is a missing value for individual i at occasion t , the conditional posterior of this missing value will depend on: a) the neighboring observations (i.e., at occasions $t - 1$ and $t + 1$); b) the individual's autoregressive parameter at the current iteration of the MCMC algorithm; and c) the uncertainty that is expressed by the residual variance (to be discussed in more detail below). This approach is similar to the way that missing data in single-subject time series analysis are handled with a Kalman smoother based on the state-space model (cf. Särkkä, 2013), and it guarantees consistent estimation as long as the missing data is missing at random.

Clearly, when there is a structural reason for certain missingness—such as no measurement during weekends as in the COGITO study, or no measurements during the night in experience sampling—it may be questionable whether this amounts to

missing at random. We will elaborate on this in the discussion.

Unequal time intervals between observations

A particular challenge when dealing with intensive longitudinal data are unequal intervals between observations. These may result from missing observations, for instance, when we have daily measurements but participants sometimes forget to fill out the end-of-day questionnaire. However, non-equidistant observations may also be a part of the research design: In experience sampling and ecological momentary assessments, participants are prompted at random time points during the day to ensure they are caught in their daily life rather than that they prepare for the next measurement. In the COGITO data, the majority of observations were obtained with an interval of one day, but there were also larger intervals, for instance because people missed a day, or because there were no measurements taken on the weekend or during holidays.³

Unequal intervals are a concern when the interest is in lagged relationships, because the strength of a lagged effect depends on the size of the time interval between the measurements (cf. Gollob & Reichardt, 1987). An elegant way of dealing with this issue is the use of continuous time models based on differential equations (Deboeck & Preacher, 2015; Voelkle, Oud, Davidov, & Schmidt, 2012), which we elaborate on in the discussion. In contrast, in discrete time models we can account for different intervals by adding missing values between subsequent observations that are made further apart in time; in doing so we create a data set in which the cases are approximately equidistant.

Heuristically, it implies that we may have a continuous time dimension with observations located on this dimension at unequal intervals. By choosing a grid, this

continuous time dimension is divided into segments of the length we specified; a smaller grid results in shorter segments. These segments are numbered 1, 2, 3, et cetera, and they either contain an observation or are assigned a missing value. Note that the actual observations could have been taken at any time within the segment they fall into, which is why the approach results in *approximately* equally spaced observations. de Haan-Rietdijk, Voelkle, Keijsers, and Hamaker (2017) found that such an approach leads to very similar results as using a modeling approach that treats time as truly continuous such that different intervals between observations are naturally accounted for. Asparouhov et al. (2017b) also includes a simulation study that shows that choosing a finer grid, such that there is a better agreement with observed times, results in good estimates despite inserting a large amount (e.g., more than 80%) of missing data.

In the current example, a logical choice is a grid based on intervals of one day, which implies that if there is an interval between two consecutive measurements of more than one day, missing values are inserted (i.e., as many as there are missing days). However, for other forms of data, such as experience sampling, the choice is less obvious, as we discuss at the end of this paper.

Model 1: A multilevel VAR(1) model for PA and NA

We begin by considering a multilevel model based on a first-order vector autoregressive (VAR(1)) model, which is represented in Figure 2. The VAR(1) model is one of the most basic time series models (for $N=1$ data), and consists of regressing a vector with observations at occasion t on the vector of observations at the preceding occasion. Multilevel extensions of this basic time series model have

emerged in the psychological literature, allowing for the analysis of multivariate time series of multiple individuals simultaneously (cf. Bringmann et al., 2013; Schuurman, Ferrer, de Boer-Sonnenschein, & Hamaker, 2016). Another way to view this model is as a multilevel extension of a cross-lagged panel model, allowing for individual differences in means and in lagged effects.

Fundamental to the use of dynamic multilevel models is that the data are decomposed into a within-person and a between-person component, as shown in Equation 1. This decomposition is also shown in the left part of Figure 2. The within-person means $\mu_{PA,i}$ and $\mu_{NA,i}$ can be thought of as a person's long-run equilibria for the variables PA and NA respectively. Such equilibria have also been interpreted as a person's trait scores, or — if we are taking a dynamic system's perspective — as the attractor of the system to which an individual returns in the absence of external perturbations. The temporal deviations from these within-person means, $PA_{it}^{(W)}$ and $NA_{it}^{(W)}$, can be thought of as the affective states of a person at occasion t .

We discuss the model specification of both parts below. Then we discuss the priors that are used in this model. Subsequently we discuss the results from these analyses for both samples.

Insert Figure 2 about here

Within-person level model

The within-person deviations $PA_{it}^{(W)}$ and $NA_{it}^{(W)}$ are regressed on themselves and each other at the preceding occasion, $PA_{it-1}^{(W)}$ and $NA_{it-1}^{(W)}$, as represented in the

top right part of Figure 2. Hence, the level 1 or within-person equations can be expressed as

$$\begin{aligned} PA_{it}^{(W)} &= \phi_{PP,i} PA_{it-1}^{(W)} + \phi_{PN,i} NA_{it-1}^{(W)} + \zeta_{PA,it} \\ NA_{it}^{(W)} &= \phi_{NN,i} NA_{it-1}^{(W)} + \phi_{NP,i} PA_{it-1}^{(W)} + \zeta_{NA,it} \end{aligned}$$

or (using the general matrix notation $\mathbf{y}_{it} = \mathbf{\Phi}_i \mathbf{y}_{it-1} + \mathbf{\zeta}_{it}$) as

$$\begin{bmatrix} PA_{it}^{(W)} \\ NA_{it}^{(W)} \end{bmatrix} = \begin{bmatrix} \phi_{PP,i} & \phi_{PN,i} \\ \phi_{NP,i} & \phi_{NN,i} \end{bmatrix} \begin{bmatrix} PA_{it-1}^{(W)} \\ NA_{it-1}^{(W)} \end{bmatrix} + \begin{bmatrix} \zeta_{PA,it} \\ \zeta_{NA,it} \end{bmatrix}, \quad (3)$$

where $\phi_{PP,i}$ and $\phi_{NN,i}$ are the autoregressive parameters for PA and NA respectively; $\phi_{PN,i}$ is the cross-lagged regression effect from NA to PA at the next occasion; and $\phi_{NP,i}$ is the cross-lagged regression coefficient from PA to NA at the next occasion.

The ζ 's represent the residuals, often referred to as *innovations*, or alternatively as *random shocks*, *disturbances*, *system noise* or *dynamic errors*. The latter term is to distinguish it from measurement error, which tends to affect the measurements only at one occasion; in contrast, dynamic error tends to change the actual course of the system, because it also affects future measurements through the lagged relationships (Schuurman, Houtveen, & Hamaker, 2015). By definition, these innovations have a mean of zero both within and between individuals. They are assumed to come from a multivariate normal distribution, that is

$$\mathbf{\zeta}_i \sim MN(\mathbf{0}, \mathbf{\Psi}^{(W)}). \quad (4)$$

Hence, at the within-person level, we estimate two variances and a covariances for the innovations.

All the lagged parameters in Equation 3 have a subject index i to indicate that individuals may differ with respect to the magnitude of these parameters. The

autoregressive parameter indicates how quickly a person restores equilibrium after being perturbed. For this reason, this parameter has also been referred to as *inertia*,⁴ *carryover*, and *regulatory weakness*. Typically, its value lies between 0 and 1, although negative values may also occur. The further away from zero this parameter is, the longer it takes a person to return to his/her equilibrium.

Individual differences in autoregressive parameters have been an important topic in empirical research. For instance, inertia in affect has been shown to be positively related to person characteristics, such as current and future depression, being female, and neuroticism (cf., Brose, Voelke, et al., 2015; Koval, Kuppens, Allen, & Sheeber, 2012; Kuppens, Allen, & Sheeber, 2010; Suls, Green, & Hillis, 1998). Others have investigated individual differences in autoregression in daily drinking behavior (Rovine & Walls, 2006).

The *cross-lagged parameters* reflect predictive relationships, and are especially interesting because they potentially represent causal mechanisms. For this reason they are sometimes referred to as *spill-over*, as they may represent the cascade effect of functioning or behavior in one domain into another domain (Almeida, Wethington, & Chandler, 1999; Bolger, DeLongis, Kessler, & Wethington, 1989; Masten & Cicchetti, 2010). However, there are two major concerns we should be aware of when considering cross-lagged parameters as evidence for causal mechanisms. First, it is very likely that there are omitted variables that vary over time and that affect both variables; the relationships found with a particular model are likely to change when such an omitted variable is included in the analysis. Second, lagged effects are specific to a particular interval between the observations, which is known as the “lag-problem” (Gollob & Reichardt, 1987); hence, a

cross-lagged parameter should never be considered “the” effect of one variable on another, but merely the effect at a particular interval (cf. Deboeck & Preacher, 2015). We elaborate on both concerns in the discussion.

Between-person level model

While the initial decomposition in Equation 1 suggests that at the between-person level we have two variables—that is, the within-person means for PA and NA (i.e., $\mu_{PA,i}$ and $\mu_{NA,i}$)—closer inspection of Equation 3 shows that we have four additional random effects, that is: two random autoregressive parameters ($\phi_{PP,i}$ and $\phi_{NN,i}$), and two random cross-lagged regression parameters ($\phi_{PN,i}$ and $\phi_{NP,i}$). If we simply consider these to be related to each other without any particular constraint, we have

$$\begin{bmatrix} \mu_{PA,i} \\ \mu_{NA,i} \\ \phi_{PP,i} \\ \phi_{PN,i} \\ \phi_{NP,i} \\ \phi_{NN,i} \end{bmatrix} = \begin{bmatrix} \gamma_P \\ \gamma_N \\ \gamma_{PP} \\ \gamma_{PN} \\ \gamma_{NP} \\ \gamma_{NN} \end{bmatrix} + \begin{bmatrix} u_{P,i} \\ u_{N,i} \\ u_{PP,i} \\ u_{PN,i} \\ u_{NP,i} \\ u_{NN,i} \end{bmatrix}, \quad (5)$$

where the six γ 's represent the fixed or averaged effects, and the six u 's represent the individual deviations from these means. These individual deviations are assumed to come from a multivariate normal distribution, that is,

$$\mathbf{u}_i \sim MN(\mathbf{0}, \mathbf{\Omega}), \quad (6)$$

where $\mathbf{\Omega}$ is a 6×6 covariance matrix. Hence, there are 6 variances (i.e., the random effects), 15 covariances, and 6 fixed effects, resulting in 27 parameters at the

between-person level. Combined with the 3 parameters estimated at the within-person level, we now have a total of 30 model parameters for this bivariate multilevel VAR(1) model.

Priors

All unknown parameters need to be given a prior distribution in Bayesian estimation. Here we make use of the defaults included in Mplus.⁵ For means and intercepts, the default is a univariate prior with mean zero and variance equal to 10^{10} . The default diffuse prior that is used in Mplus for covariance matrices is an inverse Wishart with a zero matrix for scaling and degrees of freedom equal to minus the number of variables minus 1.

For the current model we thus have the following priors. For the covariance matrix of the innovations at the within-person level, we have

$$\Psi^{(W)} \sim IW(\mathbf{0}, -3). \quad (7)$$

For the fixed effects and the covariance matrix of the random effects at the between-person level we have

$$\gamma_j \sim N(0, 10^{10}) \quad \text{where } j = \{P, N, PP, PN, NP, NN\} \quad (8)$$

$$\Omega \sim IW(\mathbf{0}, -7). \quad (9)$$

In addition to priors for these model parameters, there are also priors needed for the missing observations, and the individual parameters (i.e., the u_{ji} 's). The latter is necessary because the random effects are not integrated out.

Results

We used 50,000 iterations and two chains. Because the first half of each chain is discarded as burn-in, and because we used a thinning of 10 iterations (meaning that only 1 in 10 iterations is saved), our results here are based on 5,000 iterations (cf. Gelman et al., 2014). Model convergence is checked using the proportional scale reduction and by checking the trace plots for an absence of trends, spikes, or other irregularities. The parameter estimates for the fixed and random parameters, and their 95% credible intervals (CI) are presented in the left part of Table 1.

Only the CIs for the fixed effect $\phi_{NP,i}$ in the older sample contains zero, indicating that there is no evidence that there is an effect of PA on NA over time on average in this group. This does not necessarily imply that this is not an important parameter in the model: As it is included as a random parameter, there may be meaningful individual differences that are centered around zero. In this case, however, the variance for this parameter also seems rather small in this group, implying that the individual $\phi_{NP,i}$'s are all close to zero.⁶

To interpret the magnitude of the cross-lagged effects, we consider the standardized results that Mplus provides, which are based on standardizing the parameters per person first, and then taking the average of these. This approach was proposed in Schuurman et al. (2016) and takes into account that individuals have different cross-lagged parameter values, *and* that they may have different variances. The latter stems from the fact that the variance of a variable in the VAR(1) model is a function of the lagged parameters, which are allowed to differ across individuals. The average individually standardized lagged parameters prove to be all rather small: The average standardized effect from NA to PA is .034 (CI=[.008, .059]) in

the younger sample and .089 (CI=[.059, .119]) in the older sample; the average standardized effect from PA to NA is .038 (CI=[.017, .059] in the younger sample, and .026 (CI=[.001, .051]) in the older sample. Note that for the latter effect, the corresponding fixed effect had a CI that contained zero. This seemingly contradictory result stems from the fact that the averaged individually standardized parameter always has a smaller CI than the corresponding model parameter, which reflects the kind of inferences that can be based on them: The averaged individually standardized parameter allows for inferences conditional on the individuals in the sample (i.e., other observations within the same clusters), whereas the conventional model parameters allow for inferences to other individuals from the population. In this case, the lower bound of the CI of the average standardized effect is very close to zero, so we do not have to consider this an important contradiction.

Related to the average individually standardized regression coefficients, the standardized results also include the averaged within-person proportion of explained variance: This is .18 (CI=[.17, .20]) for PA and .21 (CI=[.19, .23]) for NA in the younger sample, and .26 (CI=[.24, .28]) for PA and .16 (CI=[.14, .17]) for NA in the older sample. Furthermore, the standardized results also reveal that the average within-person correlation between the innovations is -.19 (CI=[-.21, -.17]) in the younger sample, and -.27 (CI=[-.29, -.25]) in the older sample.

In addition to these averaged within-person standardized results, the standardized results also include the between-person level correlations between the six random effects included in the models. To represent these for both groups in a convenient and concise way, we make use of the function `qgraph` in R (Epskamp, Cramer, Waldorp, Schmittmann, & Borsboom, 2012). The resulting visual

representations included in the upper part of Figure 3 contain the correlation estimates that have credible intervals that do not include zero. Red connections represent positive (warm) correlations, and blue connections represent negative (cold) correlations; the strength of these correlations is represented by the thickness of the connections. The correlations in the younger sample ranged from .22 to .46 (in absolute values), and in the older sample they ranged from .25 to .49 (in absolute values).

Insert Figure 3 about here

These representations show that, while there are equally strong and many correlations in both samples, the patterns are very different. The two negative relationships in the correlation structure of the younger sample indicate that individuals with a higher autoregressive parameter for PA tend to have lower cross-lagged parameters from PA to NA, and individuals with a higher autoregressive parameter for NA tend to have lower cross-lagged parameters from NA to PA. The positive correlation between the autoregressive parameter for NA and the mean of NA indicates that individuals with a higher trait level for NA also tend to have more carry-over in their NA from one day to the next. Finally, the positive connection between the two means of PA and NA runs counter to the results we obtained before in the decomposition, where the between-person correlations were close to zero. The currently positive correlation implies that individuals who have a higher mean on PA also tend to have a higher mean on NA; note however that this relationship is quite weak, and further inspection of the

corresponding CI indicated that the lower bound was quite close to zero.

In contrast, in the older sample we see the correlation structure consists of two separate parts: One part connecting the parameters associated with PA, including the mean $\mu_{PA,i}$, and the lagged regression coefficients $\phi_{PP,i}$ and $\phi_{PN,i}$ (on the left side), and another part connecting the parameters associated with NA, including the mean $\mu_{NA,i}$, and the lagged regression coefficients $\phi_{NN,i}$ and $\phi_{NP,i}$ (on the right side). Higher mean PA is associated with *less* carry-over in PA, and a smaller effect from NA on PA. This pattern seems to suggest that high levels of PA are not resulting from the maintenance of PA, but that they may emerge from the ability to shield NA to spill-over into PA. In contrast, higher mean NA is associated with *more* carry-over in NA, and a stronger effect from PA to NA. Finally, the autoregressive parameter is positively correlated to the cross-lagged parameter in the same part, meaning that carry-over and spill-over are positively related.

Model 2: Extending the multilevel VAR(1) model with random innovation variances and covariance

In the model presented above we considered random means and random lagged parameters. In contrast, the innovation variances and their covariance were fixed to be equal across individuals and estimated at the within-person level, (see Equation 4). While typically within-person (or level 1) residuals are not given much thought in multilevel modeling, they are actually of great interest here: They contain everything that was not measured explicitly, but that affects the course of the variables that were observed, including social interactions, weather conditions, demands at work or at home, and physiological factors such as sugar or caffeine

intake, hormones, and health.

Here we begin by providing a brief rationale for random innovation variances and covariance. Then we discuss how to adjust the previous model to include random innovation variances and covariance. Subsequently we discuss the priors for this adjusted model. Finally, we present the results for these analyses for both samples.

Rationale for individual differences in innovation variances and covariance

As Jongerling, Laurenceau, and Hamaker (2015) argued, we may expect individual differences in the variance of this collective term, due to two kinds of differences between individuals. First, there may be individual differences in reactivity to unobserved influences. For instance, there are a number of studies that show that individuals who are depressed are characterized by larger increases in negative affect in response to external negative events than non-depressed individuals, a phenomenon that is referred to as *stress sensitivity* (Wichers et al., 2009). Similarly, non-depressed individuals are characterized by a stronger increase in positive affect in response to a positive event in comparison to depressed individuals, which is referred to as the *reward experience* (Wichers et al., 2009). Second, there may be individual differences in variability of unobserved influences. That is, some people lead more constant lives than others, and this difference in exposure to variability in external factors may also be captured by individual differences in the innovation variance.

While Jongerling et al. (2015) considered a univariate model and thus only needed a random innovation variance to account for individual differences in this part of the model, the current model is based on two variables, such that we also

have a covariance between the innovations to consider. Individual differences in the covariance between innovations can be understood as resulting from three possible sources: a) within-day effects from PA to NA; b) within day effects from NA to PA; and c) unobserved (or “third”) variables that vary over time and that affect both variables (for instance, the weather, social interactions, external demands, physiological states, etc.). In most instances, the covariance will be the result of a mix of these three sources. If we want to actually distinguish between these different explanations, we should obtain multiple measurements within a day, for instance through the use of experience sampling (cf., Conner et al., 2009). For our purposes, it is sufficient to assume that correlations between innovations are likely to result from all three sources, that is, from unobserved causes as well as within-day reciprocal effects between PA and NA. Moreover, because we believe that all these sources are likely to be characterized by individual differences, it makes sense to extend the model presented above with a random covariance between the innovations as well as random innovation variances.

Random innovation variances and covariance in the within-person level model

In the previous model, the distribution of the innovations was assumed to be identical across individuals, as is clear from the matrix $\Psi^{(W)}$ in Equation 4. Now we want to allow for individual differences in the variances and covariance of the innovations, which implies $\Psi^{(W)}$ gets a subject index i . To account for such individual differences in variances, we can use a normal distribution for the log of the innovation variance, which is the same as saying that the innovation variance comes from a log normal distribution. There are two reasons to use a log normal distribution here: a) it ensures that each individual will get a positive value for the

innovation variance; and b) it allows us to include this random effect in a multivariate normal distribution such that the random log of the innovation variance can be correlated with the other random effects such as the individual means or lagged parameters.

Extending the model with a random covariance is more complicated though, as the covariance matrix of the innovations has to be positive definite for each individual. To ensure this is the case, we make use of an additional latent variable η_{it} that represents what the two innovations have in common, while the unique parts are modeled as residuals. Specifically, the innovations are modeled as

$$\begin{bmatrix} \zeta_{PA,it} \\ \zeta_{NA,it} \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix} \begin{bmatrix} \eta_{it} \end{bmatrix} + \begin{bmatrix} \delta_{PA,it} \\ \delta_{NA,it} \end{bmatrix} \quad (10)$$

where the latter two residuals e are by definition uncorrelated; these form the unique parts of the innovations. The variances and covariance of the innovations for individual i can now be expressed as functions of the variances of the common factor and the residuals, that is,

$$\text{var}(\zeta_{PA,it}) = \text{var}(\eta_{it}) + \text{var}(\delta_{PA,it}) = \psi_i + \pi_{PA,i} \quad (11)$$

$$\text{var}(\zeta_{NA,it}) = \text{var}(\eta_{it}) + \text{var}(\delta_{NA,it}) = \psi_i + \pi_{NA,i} \quad (12)$$

$$\text{cov}(\zeta_{PA,it}, \zeta_{NA,it}) = -\text{var}(\eta_{it}) = -\psi_i. \quad (13)$$

This shows that the variances of the innovations are the sum of the unique variances and the shared variance, while the covariance between the innovations is determined by the negative variance of the common factor.

The latter is the result of choosing the factor loadings of this common factor to be 1 and -1: This implies that for each individual, the covariance between the

innovations will be negative. In the current model specification, we have to choose the innovation covariance to be either positive or negative for all individuals. This may seem needlessly restrictive or even an undesirable limitation. Alternatively, one can fix the variance of the common factor η_{it} to 1, and allowed one of the factor loadings to be estimated freely and to vary randomly across individuals: This would allow for both positive and negative covariances between the innovations. However, this alternative specification does not guarantee that every covariance matrix can be fitted well, and in our case it caused convergence problems. Another approach would be to use a Cholesky decomposition of the covariance matrix, but this option is currently not available in Mplus.

The model defined in Equations 1 and 3, combined with Equation 10, is visually represented in Figure 4. It shows that we do not estimate any parameters at level 1, but that instead, we have 9 random effects, that are estimated at the between level, which we discuss below.

Insert Figure 4 about here

Between-person level model

As indicated above, random variances are given a log normal distribution at the between-person level, such that we end up estimating the average log of the variance as the fixed effect and the variance of the log of the variance as the random effect. This way we get three additional fixed effects, that is $\gamma_{\log(\pi_{PA})}$ and $\gamma_{\log(\pi_{NA})}$ for the unique parts of the innovation variances, and $\gamma_{\log(\psi)}$ for the negative covariance between the innovations. Furthermore, we get three additional random

effects, that is two for the unique parts of the innovations, and one for the shared part.

If we simply consider all nine random effects to be related to each other without any particular constraints, the between-person level model is

$$\begin{bmatrix} \mu_{PA,i} \\ \mu_{NA,i} \\ \phi_{PP,i} \\ \phi_{PN,i} \\ \phi_{NP,i} \\ \phi_{NN,i} \\ \log(\pi_{PA,i}) \\ \log(\pi_{NA,i}) \\ \log(\psi_i) \end{bmatrix} = \begin{bmatrix} \gamma_P \\ \gamma_N \\ \gamma_{PP} \\ \gamma_{PN} \\ \gamma_{NP} \\ \gamma_{NN} \\ \gamma_{\log(\pi_{PA})} \\ \gamma_{\log(\pi_{NA})} \\ \gamma_{\log(\psi)} \end{bmatrix} + \begin{bmatrix} u_{P,i} \\ u_{N,i} \\ u_{PP,i} \\ u_{PN,i} \\ u_{NP,i} \\ u_{NN,i} \\ u_{\log(\pi_{PA,i})} \\ u_{\log(\pi_{NA,i})} \\ u_{\log(\psi_i)} \end{bmatrix}, \quad (14)$$

where the nine γ 's represent the fixed or averaged effects, and the nine u 's represent the individual deviations from these means. These individual deviations are assumed to come from a multivariate normal distribution, that is,

$$\mathbf{u}_i \sim MN(\mathbf{0}, \mathbf{\Omega}), \quad (15)$$

where $\mathbf{\Omega}$ is a 9×9 covariance matrix, which implies there are 9 variances (i.e., the random effects), and 36 covariances. Combining this with the 9 fixed effects, we now have a model with 54 parameters at the between-person level.

Priors

The current model only has parameters at the between-person level. The default priors for the nine fixed effects are

$$\gamma_j \sim N(0, 10^{10}) \quad (16)$$

where $j = \{P, N, PP, PN, NP, NN, \log(\pi_{PA,i}), \log(\pi_{NA,i}), \log(\psi_i)\}$. The default prior for the covariance matrix of the random effects is

$$\mathbf{\Omega} \sim IW(\mathbf{0}, -10). \quad (17)$$

Results

Again, we used 50,000 iterations and a thinning of 10. The parameter estimates and their 95% credible intervals are presented in the right part of Table 1. Note that none of these intervals includes zero, indicating that there is ample evidence that these fixed effects differ from zero.

We also visually represented the correlations between the 9 random effects in the lower part of Figure 3. When comparing these to the correlation structures based on Model 1, it is striking that the relationships between the random effects that are included in both models (i.e., means and lagged parameters) change depending on whether or not the variances and covariance of the innovations are included as random effects. This underscores the need to consider potential randomness in these residual variances, because ignoring these additional sources of individual differences may result in biased estimates of the other model parameters, as was also shown by Jongerling et al. (2015).

When comparing the correlation structures of the two samples based on Model 2, it is clear that the younger sample is characterized by more correlations than the

older sample. However, there are also some similarities across the two groups. First, what is interesting to see is that both groups are characterized by strong positive connections between the individual's mean on NA (i.e., $\mu_{NA,i}$), the unique part of the innovation variance of NA (i.e., $\log(\pi_{NA,i})$), and the log variance of the factor that represents the negative covariance between the innovations of PA and NA (i.e., $\log(\psi_i)$). This implies that individuals with a relatively high mean on NA also tend to be characterized by a larger innovation variance (as this is the sum of $\pi_{NA,i}$ and ψ_i , see Equation 12), and a stronger negative covariance between the innovations (as the covariance between the innovations is obtained by taking the exponential of $\log(\psi_i)$ and multiplying this by -1, see Equation 13).

Second, in both groups there are also relatively strong positive relationships between the autoregressive coefficient for NA (i.e., $\phi_{NN,i}$), the mean of NA (i.e., $\mu_{NA,i}$), and the unique part of the innovation variance of NA (i.e., $\log(\pi_{NA,i})$). This implies that individuals who are relatively high on NA on average, tend to be characterized by a stronger carry-over effect for their NA, and they have larger (unique) innovation variances.

Third, in both groups there are positive relationships between the log of the unique variances of PA and NA (i.e., $\log(\pi_{PA,i})$ and $\log(\pi_{NA,i})$) on the one hand, and the log of the negative covariance between the innovations of PA and NA (i.e., $\log(\psi_i)$). This implies that ψ_i is also positively related to $\pi_{PA,i}$ and $\pi_{NA,i}$, which means that individuals who are more reactive to external influences and/or who experience more variability in external influences, tend to do so for both PA and NA (as the innovation variance of PA is the sum of $\pi_{PA,i}$ and $\log(\psi_i)$, and the innovation variance of NA is the sum of $\pi_{NA,i}$ and $\log(\psi_i)$; see Equations 11 and 12).

Fourth, there is a negative correlation between the mean of PA (i.e., $\mu_{PA,i}$) and the lagged effect from NA to PA (i.e., $\phi_{PN,i}$) in both samples. This implies that individuals who are relatively high on PA on average, tend to be characterized by a lower cross-lagged effect from NA to PA.

Finally, there is a negative relationship in both groups between the autoregressive parameter of PA (i.e., $\phi_{PP,i}$), and the negative covariance between the innovations. This implies that when individuals are characterized by more carry-over in their PA, they also tend to have a smaller value for the log of the negative covariance, which corresponds to larger negative covariance between the innovations.

While the current approach makes it easy to investigate the relationships between all the random effects in the model, this also leads to an increased complexity: Where we started with just two observed variables in the original decomposition, we now have nine random effects and 36 correlations between them. Alternatively however, one may also argue that where we started out with a dataset of $2 \times 100 \times 100$ (i.e., variables by persons by time points), we have now reduced this to a an 9 by 9 correlation matrix.⁷ Either way, this is still a large number of relationships, which we may want to model further, for instance by using predictors or latent variables to account for their interrelatedness. We consider one particular approach next.

Model 3: Indirect effects through the random effects

As in most intensive longitudinal data sets, the COGITO study includes diverse person characteristics that were measured prior and/or after the intensive

longitudinal measurement period. Here we consider depressive symptoms measured by the Center for Epidemiologic Studies Depression (CESD) scale both before and after the daily measurement phase. Prior research, including analysis of this issue with the data from the COGITO study (cf. Brose, Schmiedek, Koval, & Kuppens, 2015), has shown that the autoregressive parameter of affective measurements is positively related to current levels of depression, but also that it is predictive of depression two and a half years later, suggesting that it flags an important malfunctioning regulation mechanism (Houben, Van den Noortgate, & Kuppens, 2015; Koval et al., 2012; Kuppens et al., 2010; Kuppens et al., 2012). To see whether we can replicate these two findings in a single model, we include pre-CESD as a predictor of the nine random effects of the dynamic multilevel model described above, and post-CESD as an outcome variable of these random effects and of pre-CESD. We compute additional parameters in Mplus, based on a product of the two parameters that form an indirect effect through a particular random effect. This allows us to investigate these nine indirect effects, using their posterior distributions.

In Table 2, we have included the point estimates and the 95% CIs for the nine indirect effects and the direct effect. It shows that in both samples there is a positive *direct effect* of pre-CESD on post-CESD, with the effect in the older sample being about twice as large as that in the younger sample. Furthermore, in the younger sample there is evidence that two of the nine *indirect effects* are different from zero. The first of these is through the autoregressive parameter of NA (i.e., ϕ_{NN}), which confirms previous findings (Brose, Schmiedek, et al., 2015; Kuppens et al., 2012): People with more depressive symptoms at the start (i.e., higher pre-CESD), tend to have more carryover of negative affective states (i.e., higher

autoregression in NA), which in turn is associated with more depressive symptoms at the post-assessment (i.e., higher post-CESD). This effect exists after controlling for previous depression (i.e., the direct effect). The second indirect effect is through the covariance of the innovations, and illustrates the importance of looking past the usual suspects of means and autoregression: It implies that higher pre-CESD precedes a stronger negative covariance between the innovations (either because of within day reciprocal effects or because of an unmeasured common cause), which is followed by higher post-CESD. This latter result is in agreement with the idea that people who differentiate less in their affective responses (i.e., individuals with a larger negative covariance between innovations), run more risk of becoming depressed (cf. van Borkulo, Boschloo, Borsboom, Penninx, & Schoevers, 2015).

The two indirect effects added together are 0.199, which is about two-thirds of the direct effect, which is 0.290. Moreover, note that there were no indirect effects through the individual means of PA and NA of prior depressive symptoms on later depressive symptoms. In the younger sample, only the mean of NA was related to pre-CESD (point estimate and 95% CI: 0.78 [0.34,1.25]), whereas in the older sample the mean of PA was related to pre-CESD (point estimate and 95% CI: -2.00 [-2.94,-1.02]); none of the means were predictive of post-CESD. Although highly speculative, the largely absent association between depression scores and average PA and NA from the daily measurements may reflect a form of adaption in scale use, where depressed individuals grow used to feeling more NA and less PA, and thus change their reference point when filling out daily diaries.

Discussion

We have used the COGITO affect data to showcase some of the exciting new possibilities there are to analyze intensive longitudinal data. While dynamic multilevel modeling has been applied more often in recent years, the current approach forms a unique combination of a number of key features that make it particularly appealing, that is: a) it is based on multivariate data, allowing for multiple dependent or outcome variables; b) it handles missing data using MCMC sampling; c) it handles unequal intervals by making the observations (approximately) equally spaced through adding missing values; d) it gives results that are standardized per person, such that the relative strength of cross-lagged parameters can be compared; e) it allows for random variances and covariances, which are to be expected from a substantive viewpoint; and f) it allows for modeling the random effects at the between-person level, through considering these as outcome variables, but also as predictors.

Along the way, we have identified a number of questions that are likely to arise when taking a dynamic multilevel modeling approach. As we stated at the start, there are very few guidelines and rules of thumb for this approach; this stems from the fact that dynamic multilevel modeling is still in its infancy. To some extent, practices from other fields—such as traditional single-subject time series analysis—may be appropriate. However, we need to carefully evaluate how these will apply in the context of multilevel extensions. Moreover, we also need to consider their relevance for psychological research, as the goals one pursues here may differ from the goals in disciplines like econometrics.

Here we provide a brief treatment of the issues identified before, and include a

few additional concerns that we believe to be most urgent. For ease of presentation, we have grouped these into three categories: a) data requirements; b) model evaluation; and c) theoretical concerns. Although we should not expect easy and clear cut solutions for many of these problems, it is paramount to the field and its progress to consider these issues in the years ahead.

Data requirements

Sample size. More needs to be known about the trade-off between the number of people, the number of time points, the number of variables, and the number of random effects and other parameters in the model. This will clearly depend on the circumstances, and we should not expect a one-size-fits-all rule of thumb. However, general knowledge regarding reasonable ratios between these quantities would be extremely useful for researchers who wish to set up an intensive longitudinal study and wonder whether they should invest in more participants or more time points per participant.

One way in which such knowledge can be developed is through simulation studies that investigate the accuracy and reliability of parameter estimates, coverage rates, and efficiency. This can be done for basic models that are likely to be used frequently, but it could also be tailored to a particular research design, similar to a power study. For a first simulation study of this kind, see Schultzberg and Muthén (in press).

Non-normal data. As indicated in the introduction, we assumed all data were normally distributed, both within and between individuals. However, it is well known that measures of negative affect tend to be non-normal. More specifically,

the within-person distribution for some individuals may look quite normal, but many other individuals are characterized by a strong floor effect in that they indicate at a large number of occasions that they experience no negative affect at all (cf. Brose, De Roover, Ceulemans, & Kuppens, 2015).

How to deal with such distributions continues to be a challenging question. Potential solutions could be to handle such variables as categorical (i.e., ordinal) rather than as continuous, to use latent variables with multiple indicators rather than sum scores, or a combination of these two (i.e., use ordinal indicators of a continuous latent variable). All these options are available in the current version of DSEM in Mplus, but they have not been studied extensively and compared yet. Another possible approach would be to use a regime-switching model, in which individuals switch between different states according to a hidden Markov model, which can be estimated using a continuous observed variable (cf. Kim & Nelson, 1999; Hamaker, Grasman, & Kamphuis, 2016). A multilevel extension of this approach will be possible with a future version of Mplus (see Asparouhov et al., 2017a).

Model evaluation

Alternative models. First-order autoregressive models—like the ones used in the current empirical application, but also first-order differential equations—can be considered a very basic approach to study dynamics, and it is without a doubt the most frequently used approach for studying processes in the social sciences. However, there are many alternative models in the dynamic modeling literature on time series analysis and differential equations. These include higher-order autoregressive (or differential) models, models with moving average terms,

integrated models (based on difference scores), models with measurement error, and models that allow for regime switching (Chatfield, 2004; Hamilton, 1994).

While some of these models have been used in dynamic multilevel analyses, allowing for individual differences in the dynamics parameters through modeling these as random effects at level 2 (cf., Asparouhov et al., 2017a, 2017b; de Haan-Rietdijk, Gottman, Bergeman, & Hamaker, 2016; Wang et al., 2012), this area is still largely unexplored. However, the need to move beyond first-order autoregressive models is undeniable, whether the interest is in mere prediction or in actually understanding the underlying mechanism. As we expand the kinds of models we wish to consider, the need will increase to evaluate their fit and compare them.

Model comparison. There is a need for measures that can be used to compare nested and non-nested models. A commonly used measure in Bayesian analysis is the deviance information criterion (DIC; Spiegelhalter, Best, Carlin, & van der Linde, 2002), which is also reported when using DSEM. However, it is not functioning optimally for these models, due to the many parameters that need to be sampled: All the individual parameters are also treated as unknown parameters in the Bayesian context, which have to be sampled at each iteration, and this makes the DIC very unstable, even when very large numbers of iterations are used. Moreover, because the DIC is based on a likelihood in which the random effects are included, the DIC is not always comparable across models due to the parametrization (cf. Celeux, Forbes, Robert, & Titterton, 2006).

Alternatively, we can check whether there is evidence that a parameter differs from zero based on its CI, but for variance terms, these will never include zero by

definition. Hence, at this point there is no easy to use tool to determining whether a random effect is necessary, or that the variance across individuals can be fixed to zero.

Model fit. Related to model comparison, there is also a need for measures to evaluate model fit. This may prove rather challenging, as even in $N=1$ time series analysis, there is not a strong tradition of summarizing model fit. This may be because the focus in time series analysis is not specifically on the proportion of explained variance (as it tends to be in regression analysis), but also on the autocovariance structure of the data, and this includes all lags (from lag 0 up to lag $T - 1$ for a series of length T). As a result, here is no saturated model that could serve as a basis for comparison as is typically done in structural equation modeling.

Evaluating the appropriateness of a time series model has often relied on investigating whether the residuals (i.e., innovations) behave like white noise, meaning there are no autocorrelations in these series (Box, Jenkins, Reinsel, & Ljung, 2016): This illustrates the strong focus on trying to capture the autocovariance structure in the observed data. In multilevel multivariate extensions, this implies we have to consider the autocorrelation and partial autocorrelation functions for each variable and the cross-lagged correlations functions for each pair of variables for each person: Clearly, it will not be easy to keep track of the many functions, and even more so, it would also require the development of new rules of thumb regarding—for instance—the number of acceptable violations of the white noise assumption.

Theoretical concerns

Causality. Although the topic is often not discussed explicitly, researchers in the social sciences who use longitudinal data are often interested in the causal relationships between variables. While longitudinal data allows for temporal order—such that a potential cause precedes its assumed effects in time—these are nevertheless observational data, which implies that the omitted variable problem hampers causal conclusions. In this regard, it is helpful to distinguish between time-invariant and time-varying omitted variables.

Time-invariant omitted variables are of no concern when using either a single subject approach, because it is a constant in that context. Similarly, when we have multilevel longitudinal data, the decomposition into a between-person and a within-person part like we discussed at the beginning of this paper, ensures that the time-invariant omitted variables are separated from the within-person dynamics (see also Allison, 2009; Halaby, 2004; Hamaker, Kuiper, & Grasman, 2015; Ousey, Wilcox, & Fisher, 2011). However, time-varying omitted variables are still a major concern when our interest is in causal mechanisms that we hope to understand better by evaluating the within-person part.

In the time series literature, the concept of Granger causality is often brought up, but the opinions are divided on how useful it is as a basis for causal conclusions. Eichler (2013) and Eichler and Didelez (2010) have connected diverse definitions of causality, including Granger causality and interventionism in the context of time series. There have also been innovations in the area of design, referred to as micro-randomization, in which an intervention is randomly assigned to time point (Klasnja et al., 2015). This approach has been used in health research, for instance

to stimulate participant to be more physically active. Other recent developments have used time series models in combination with impulse response functions to generate feedback for participants about how they may generate for instance a 10% increase in one variable by changing another variable (Blaauw, van der Krieke, Emerencia, Aiello, & de Jonge, 2017). Hence, in the latter case, the time series model is used to generate hypotheses that professionals may use to design a person-tailored intervention for a particular individual.

Trends and cycles. Closely related to the concern of omitted time-varying variables, is the issue of trends and cycles in the data. In the time series literature, the convention is to de-trend data before considering further relationships between variables (e.g., Chatfield, 2004), and this approach has also been advocated by some in panel research and intensive longitudinal studies (e.g., Berry & Willoughby, 2016; Curran & Bauer, 2011; Wang et al., 2012). Wang and Maxwell (2015) showed that when the interest is in the effect of a predictor on an outcome in longitudinal multilevel models, it does not matter whether one detrends the predictor, detrends the predictor and the outcome, or includes time as a covariate without detrending the predictor or the outcome. However, the results can differ starkly from those obtained when the trend is not accounted for in one of these ways.

As pointed out by Wang and Maxwell (2015) and Y. Liu and West (2016), how we handle potential trends and cycles in the data, is likely to have serious consequences for the parameter estimates that describe the dynamics of the process and the predictive relationships between variables over time: It should therefore reflect our conviction of the underlying mechanism, and whether we believe trends and cycles are something that happens separately from the dynamics, or as an

intrinsic part of it. In the latter case, one may actually prefer not to explicitly model trend or cycles, but simply allow these to emerge as part of the dynamics of a model. The latter approach is common in the dynamic systems literature, where long-term trends are assumed to result from the same underlying dynamics as the short-term fluctuations (cf. Bisconti et al., 2004; Van der Maas et al., 2006; Voelkle et al., 2012).

The models used in this paper could be extended with trends or cycles over time by adding this as a within-person level predictor. As shown by Wang and Maxwell (2015), whether this approach is used, or the relationships are modeled between the residuals of the variables (after the trends are account for), makes little difference (see also Hamaker, 2005). Alternatively, trends could be accounted for through the cross-classification option offered by DSEM (see Asparouhov et al., 2017b); this approach accounts for the average (across individuals) trend over time in an exploratory manner, meaning the researcher does not have to decide on the shape such as linear, sine wave, etcetera. Alternatively, we can add time as a predictor and allow for a random slope so that individuals can be characterized by different trends. However, when individuals are characterized by (very) different trends, or are not in sync in their cycles, this approach would not be appropriate, and it is better to use the explicit modeling of it at the within-person level.

Between-person differences. As shown in Models 1 and 2, even with a relatively simple bivariate dataset, we can easily obtain a rather complex covariance structure at the between-person level. Some have proposed to use the within-person means to construct between-person networks that can be used as a tool for making causal inferences (Epskamp, Waldorp, Mottus, & Borsboom, 2017). However, like

the time-varying omitted variables are a threat to causal inference at the within-person level, time-invariant omitted variables are a major concern when wishing to draw causal conclusions at the between-person level.

Nevertheless, these modeling opportunities challenge researchers to think about their theories in new ways, and to become more precise about their hypotheses: Do they assume their theory pertains to the within-person level or the between-person level, and at what timescale do they expect particular relationships to appear? Such considerations can guide the modeling approach, but may also have important implications for the way the data should be gathered.

Discrete versus continuous time. The results that are obtained with discrete time models such as the VAR(1) models used in this study, are specific to a particular time interval. While for daily diary data, where individuals are asked to provide an average of their experiences for the entire day, this approach may be considered appropriate, it is more problematic when the data consist of momentary experiences, such as obtained with for instance experience sampling or ecological momentary assessments. In such approaches, the measurements are taken at random intervals, which reflects the underlying assumption that the process actually evolves continuously over time and could be measured at any time point.

An alternative modeling approach that has been used for such data is continuous time modeling (Oravecz, Tuerlinckx, & Vandekerckhove, 2011; Voelkle et al., 2012). These models are based on differential equations and instead of estimating the lagged effects for a particular interval as we do in discrete time models, continuous time models result in a drift matrix that represents the expected change (i.e., the first-order derivatives) as a function of the current values of the

variables in the system (Boker & Laurenceau, 2006; Oud, 2007). Thus, compared to discrete time models, continuous time models have the advantage that they naturally account for unequal intervals between the observations (including missing observations), and that the resulting parameters do not pertain to a particular interval that was used in the analysis.

It should be noted however that there are mathematical relationships between the drift matrix that is obtained with continuous time analysis, and the matrix for lagged coefficients from a discrete time analysis, such that even when a discrete time analysis is executed, the results can be converted to what they would be when a continuous time analysis had been run instead (Deboeck & Preacher, 2015; de Haan-Rietdijk et al., 2017; Voelkle et al., 2012). At a more fundamental level, however, the discrete versus continuous time distinction raises the question of how the results of lagged models are best represented: Should we provide the result that are related to a particular lag, or consider an alternative representation related to the continuous time perspective, such as the drift matrix, vector fields (Boker & McArdle, 2014), or curves of the value particular parameters take on at different intervals (e.g. Deboeck & Preacher, 2015)? While all these representations are based on the same information, the relatedness between them may be hard to grasp for researchers who are not that familiar with dynamic systems analyses, and it is not clear which of these representations is most intuitive and valuable in the context of applied research. Nevertheless, it is important that researchers in this area recognize the limitations of only focusing on the lagged parameters obtained from a discrete time analysis.

Structural missings due to nighttime or weekends. In the COGITO data, no observations were made during weekends or holidays. Such structural missings are quite common in intensive longitudinal data. For instance, in experience sampling, which is based on multiple measurements per day, typically no measurements are taken during the night. In the current approach we assumed that the process just continued during the missing episodes. Alternatively, instead of dealing with these data as two-level with observations nested in individuals, we can also consider them as three-level with repeated measures nested in days or weeks, which are subsequently nested in individuals.

de Haan-Rietdijk, Kuppens, and Hamaker (2016) compared the two-level and three-level approach in the context of experience sampling data, where the two-level model consists of measures nested in persons, and the three-level model consists of beeps nested in days which are nested in persons. The results showed that autoregression in a two-level model may result from ignoring the three-level structure of the data, but that it is also possible to detect an additional level as the result of autoregression in a two-level model. Their empirical application showed more evidence for the two-level than the three-level model, but clearly more research is needed with diverse data sets and data collection protocols.

To conclude

With the many novel modeling opportunities that have appeared recently for the analysis of intensive longitudinal data, we also see many new challenges and unresolved issues that require solutions. However, we should not let this discourage us at this point. Rather, it is our hope that the fast technological and statistical developments that are taking place now will inspire many of us to pursue a research

line in this innovative field: We need psychometricians, applied statisticians, quantitative psychologists and substantive researchers to explore this exciting new frontier, so that ten years from now we can look back and smile at how little was known today.

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Table 1: Point estimates (posterior means) and 95% credible intervals for fixed effects (i.e., means) and random effects (i.e., variances) in both groups.

Variable	Model 1						Model 2					
	Fixed Effects (means)		Random Effects (variances)		Fixed Effects (means)		Random Effects (variances)		Fixed Effects (means)		Random Effects (variances)	
	Young	Older	Young	Older	Young	Older	Young	Older	Young	Older	Young	Older
$\mu_{PA,i}$	3.09 [2.88,3.31]	4.56 [4.28,4.83]	1.18 [0.87,1.62]	1.86 [1.39,2.54]	3.10 [2.88, 3.32]	4.58 [4.29, 4.85]	1.27 [0.94,1.74]	1.96 [1.45,2.72]	3.10 [2.88, 3.32]	4.58 [4.29, 4.85]	1.27 [0.94,1.74]	1.96 [1.45,2.72]
$\mu_{NA,i}$	0.98 [0.83,1.13]	0.32 [0.21,0.42]	0.60 [0.44,0.83]	0.30 [0.22,0.41]	0.97 [0.82, 1.13]	0.31 [0.21, 0.43]	0.60 [0.44,0.85]	0.31 [0.23,0.43]	0.97 [0.82, 1.13]	0.31 [0.21, 0.43]	0.60 [0.44,0.85]	0.31 [0.23,0.43]
$\phi_{PP,i}$	0.33 [0.28,0.39]	0.42 [0.36,0.47]	0.06 [0.04,0.08]	0.06 [0.05,0.09]	0.37 [0.32, 0.42]	0.47 [0.42, 0.53]	0.06 [0.04,0.08]	0.07 [0.05,0.10]	0.37 [0.32, 0.42]	0.47 [0.42, 0.53]	0.06 [0.04,0.08]	0.07 [0.05,0.10]
$\phi_{PN,i}$	0.05 [0.01,0.09]	0.17 [0.09,0.25]	0.02 [0.01,0.04]	0.10 [0.07,0.16]	0.08 [0.04, 0.13]	0.15 [0.07, 0.24]	0.03 [0.02,0.05]	0.07 [0.04,0.13]	0.08 [0.04, 0.13]	0.15 [0.07, 0.24]	0.03 [0.02,0.05]	0.07 [0.04,0.13]
$\phi_{NP,i}$	0.04 [0.01,0.07]	0.02 [-0.02,0.06]	0.01 [0.01,0.02]	0.03 [0.02,0.04]	0.03 [0.00, 0.06]	0.02 [0.00, 0.03]	0.01 [0.00,0.01]	0.00 [0.00,0.00]	0.03 [0.00, 0.06]	0.02 [0.00, 0.03]	0.01 [0.00,0.01]	0.00 [0.00,0.00]
$\phi_{NN,i}$	0.37 [0.32,0.42]	0.23 [0.17,0.29]	0.06 [0.04,0.09]	0.06 [0.05,0.09]	0.40 [0.34, 0.45]	0.27 [0.22, 0.33]	0.07 [0.05,0.09]	0.06 [0.05,0.09]	0.40 [0.34, 0.45]	0.27 [0.22, 0.33]	0.07 [0.05,0.09]	0.06 [0.05,0.09]
$\log(\pi_{PA,i})$					-1.33 [-1.51,-1.17]	-2.53 [-2.75,-2.32]	0.69 [0.50,0.97]	1.18 [0.88,1.62]	-1.33 [-1.51,-1.17]	-2.53 [-2.75,-2.32]	0.69 [0.50,0.97]	1.18 [0.88,1.62]
$\log(\pi_{NA,i})$					-2.04 [-2.33,-1.75]	-4.37 [-4.73,-4.01]	1.92 [1.39,2.71]	3.30 [2.44,4.55]	-2.04 [-2.33,-1.75]	-4.37 [-4.73,-4.01]	1.92 [1.39,2.71]	3.30 [2.44,4.55]
$\log(\psi_i)$					-3.29 [-3.64,-2.98]	-4.78 [-5.09,-4.43]	2.00 [1.40,2.95]	2.60 [1.92,3.60]	-3.29 [-3.64,-2.98]	-4.78 [-5.09,-4.43]	2.00 [1.40,2.95]	2.60 [1.92,3.60]

Model 1 is the multilevel VAR(1) model with random means for daily positive and negative affect ($\mu_{PA,i}$ and $\mu_{NA,i}$), and random autoregressive and cross-lagged regression coefficients ($\phi_{PP,i}$ to $\phi_{NN,i}$). Model 2 also includes random log of the variance of the unique parts of the innovations ($\log(\pi_{PA,i})$ and $\log(\pi_{NA,i})$); and random log of the negative covariance between the innovations ($\log(\psi_i)$).

Table 2: Point estimates (posterior means) and 95% credible intervals for direct and indirect effects of pre-CESD on post-CESD in both groups.

Effect	Young	Older
direct	0.290 [0.062,0.522]	0.585 [0.076,1.206]
through $\mu_{PA,i}$	0.058 [-0.011,0.154]	0.055 [-0.018,0.147]
through $\mu_{NA,i}$	0.024 [-0.062,0.130]	0.011 [-0.020,0.070]
through $\phi_{PP,i}$	0.003 [-0.032,0.050]	0.003 [-0.020,0.043]
through $\phi_{PN,i}$	0.000 [-0.053,0.061]	-0.004 [-0.111,0.102]
through $\phi_{NP,i}$	-0.019 [-0.178,0.087]	-0.046 [-0.820,0.454]
through $\phi_{NN,i}$	0.127 [0.036,0.258]	-0.011 [-0.068,0.021]
through $\log(\pi_{PA,i})$	0.000 [-0.059,0.055]	-0.045 [-0.131,0.005]
through $\log(\pi_{NA,i})$	-0.009 [-0.103,0.076]	0.074 [-0.017,0.200]
through $\log(\psi, i)$	0.072 [0.004,0.185]	0.031 [-0.035,0.122]

The nine random effects are: the means of daily positive and negative affect ($\mu_{PA,i}$ and $\mu_{NA,i}$); the autoregressive and cross-lagged regression coefficients ($\phi_{PP,i}$ to $\phi_{NN,i}$); the log of the variance of the unique parts of the innovations ($\log(\pi_{PA,i})$ and $\log(\pi_{NA,i})$); and random log of the negative covariance between the innovations ($\log(\psi_i)$).

Footnotes

¹At this point, multiple group analyses are not part of DSEM in Mplus version 8 yet. Alternatively, we could treat the data as one sample, and have a grouping variable that is used at the between-person level to see whether there are differences between the groups. However, as the two samples were sampled from different age populations, we decided to treat them as two separate samples here.

²Brose et al. (2013) actually investigated the effect of current affective state on the way individuals answer questions with respect to what they are like in general (i.e., when they are given a trait instruction), using data from the COGITO study. The results showed that the current affective state a person is in contributed substantially to the way a person evaluates their general affect. It is likely that the relative contributions of trait and state depend on the instruction that is given, but studies like the one by Brose et al. (2013) show that using a particular instruction does not eliminate the potential contamination of other sources of variability.

³In the younger sample, for instance, the intervals were 1 day for 10,066 cases, 2 days for 7,321 cases, 3 days for 1,580 cases, 4 days for 636 cases, 5 days for 168 cases, 6 days for 89 cases, 7 days for 54 cases, and so on, with a maximum interval of 54 days.

⁴While inertia is a term that has been used extensively to refer to autoregression and autocorrelation in affective research, starting with Suls et al. (1998) and Gottman, Murray, Swanson, Tyson, and Swanson (2002), this should not be confused with the usage of this term in the context of differential equations and physics.

⁵These are obtained as part of the output in Mplus when asking for the

TECH1 output.

⁶Note that the CI of a variance term will never include zero, as the prior is specified to be larger than zero. Hence, using the CI of a variance estimate to investigate whether there is evidence that a parameter differs from zero, is not as straight forward as it is for other parameters.

⁷The authors thank Nilam Ram for pointing out this alternative perspective.

Figure Captions

Figure 1. Variance estimates for the younger and older samples, with the corresponding standard errors, including: 1) total variance (across time and persons); 2) between-person variance (i.e., variance in within-person means across people); and 3) within-person variance (i.e., variance within people across time). For each variable in each group, we also included the intraclass correlation (ICC), which represents the proportion of total variance that is account for by the stable between-person differences.

Figure 2. Representation of the multilevel VAR(1) model. Left part contains the decomposition into within-person (time-varying) and between-person (time-invariant) components. Top right contains the within-person level model, which is a VAR(1) model. Bottom right contains the between-person level model, which includes the between-person components from the decomposition, as well as all the random effects of the model, corresponding to the solid black circles in the within-person level model.

Figure 3. Visual representations of the correlation structure of the random effects of the multilevel VAR(1) models in the two samples. Upper part contains the correlations between the six random effects in model 1, while the bottom part contains the correlations between the nine random effects of model 2. Only correlations whose 95% credible interval did not include zero are included here. Red connections represent positive correlations, blue connections represent negative correlations. Strength of the correlations is represented by the thickness of the connection.

Figure 4. Representation of the multilevel VAR(1) model with random innovation variances and covariance. Left part contains the decomposition into within-person (time-varying) and between-person (time-invariant) components. Top right contains the within-person level model, which is a VAR(1) model. Bottom right contains the between-person level model, which includes the between-person components of the observed data as well as all the random effects of the model, corresponding to the solid black circles in the within-person level model. It shows that random variances at the within-person level are modeled using their log at the between-person level (which are then assumed to come from a multivariate normal distribution); this is done to ensure that the individual variances are positive for all individuals.







